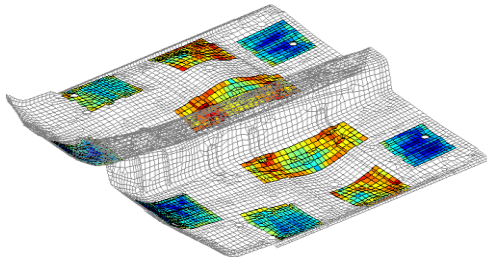
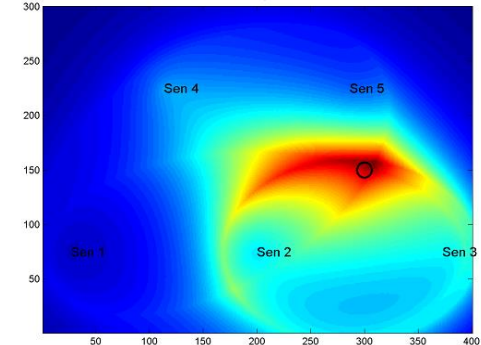




DAMAGE TOLERANT ACTIVE CONTROL: *CONCEPT AND APPLICATIONS*



Mechbal Nazih

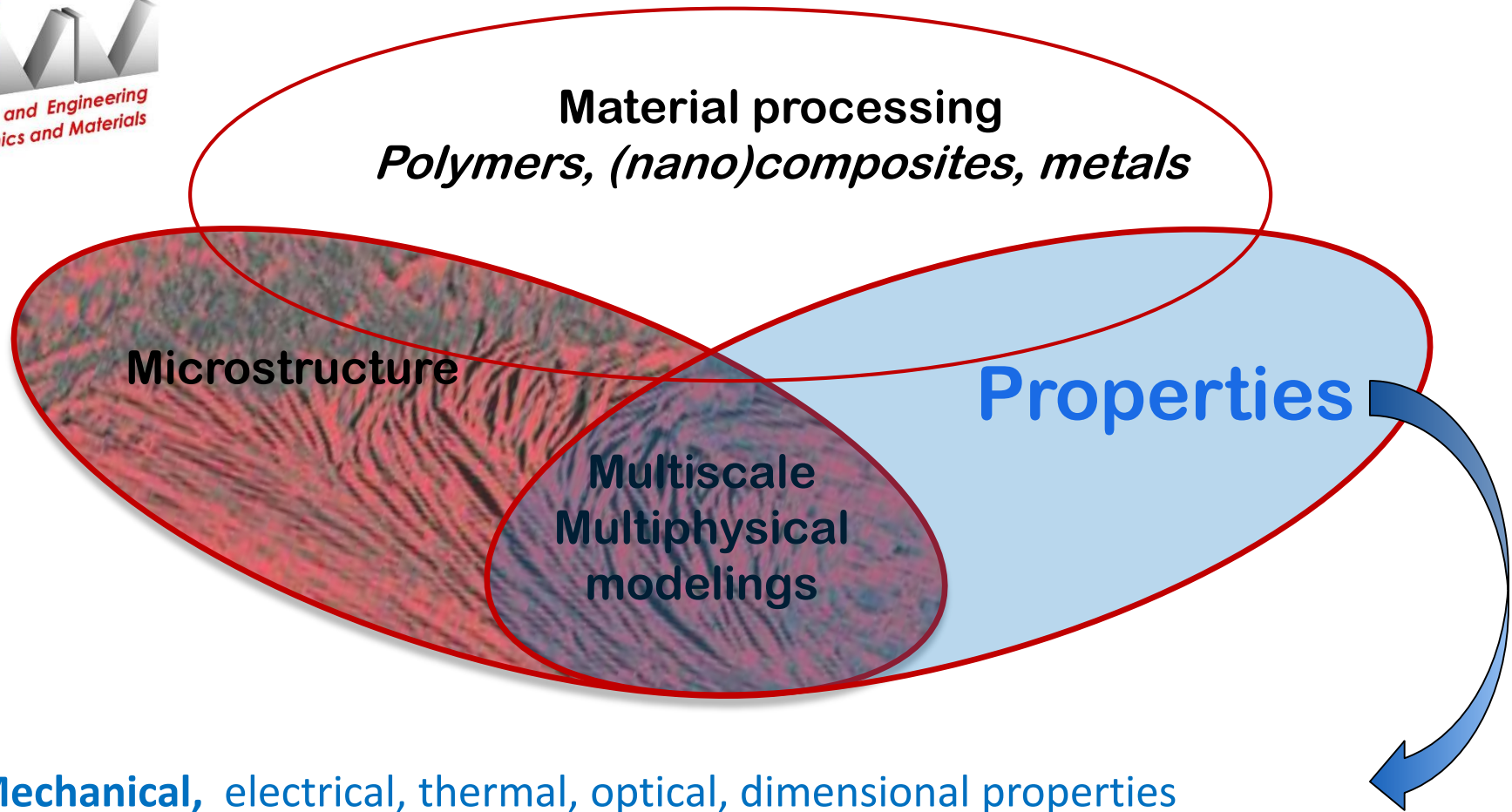


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1ERE JOURNEE NATIONALE CONTROLE SANTE ET MONITORING DES
STRUCTURES

15 Mars 2018



- **Mechanical**, electrical, thermal, optical, dimensional properties
- **Long-term properties**: durability of polymers, composite, gigacycle fatigue of steel

Multidisciplinary competences

From chemistry to mechanics and **control**, from experimental to numerical simulations



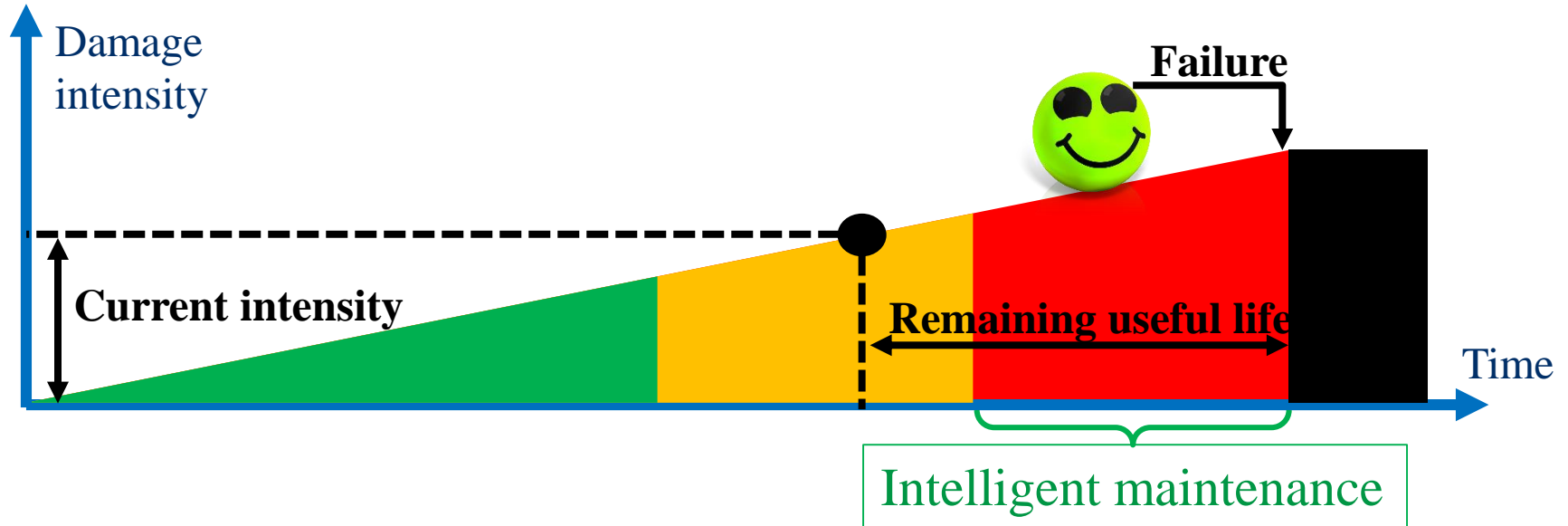
- **Introduction and Motivation**
- **Damage Tolerant Active Control (DTAC)**
- **DTAC Strategies & Examples**
- **Conclusion**



- **Introduction and Motivation**
- **Damage Tolerant Active Control (DTAC)**
- **DTAC Strategies & Examples**
- **Conclusion**

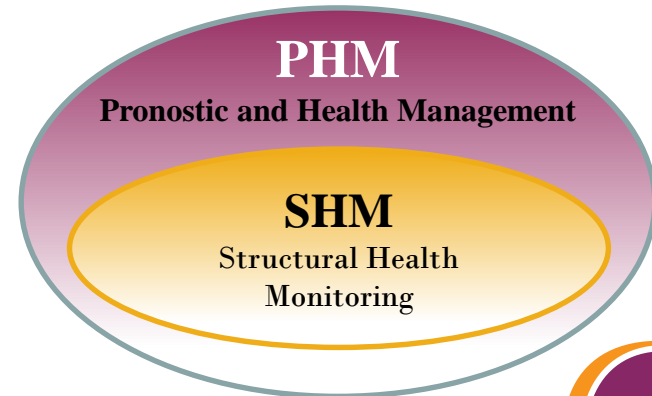
WHY DTAC ?

✿ Increasing the availability: intelligent maintenance



✿ Need for a solution to:

- Assess the current damage intensity
- Infer the remaining useful life (**RUL**)



WHY DTAC ?



✶ Vibrations ...

➤ are recurring problems in means of land and air transport.

Cost reduction



Lightweight structures



✶ Damages ...

Accidental

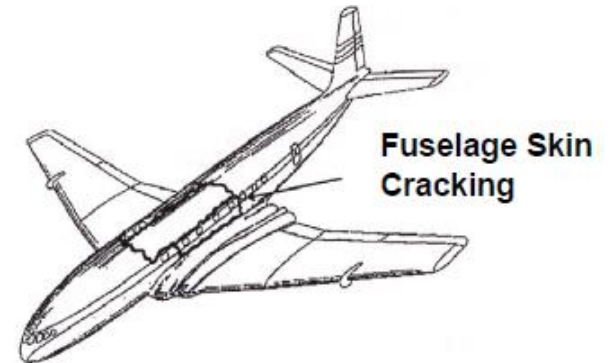


Impacts



✶ Aging and fatigue ...

Corrosion



1290 flight cycles

WHY DTAC ?



✿ A question:

Without compromising safety, could we make our structures:

- Better available?
- Lighter weight?
- More cost efficient?
- More reliable?
- More sustainable ?



✿ A response is : Smart structures ...

- which is the integration of *sensing and possibly also actuation* devices seeking to satisfy several characteristics of a biological system as sensing, actuation, adaptability and self-repair ...

✿ ... with SHM (Structural Health Monitoring)

- which is the integration of smart devices allowing the loading and damaging conditions of a structure to be *recorded, analyzed, localized and predicted* in a way that *non-destructive testing becomes an integral* part of the structure ...

✿ ... and Active Control capabilities

- that will permit to reduce noises and to *minimize mechanical vibrations* of structures *preventing from prejudicial damage* provoked by excessive strain or by fatigue



Damage Tolerant Active Control
(Contrôle Actif Tolérant aux Dommages)



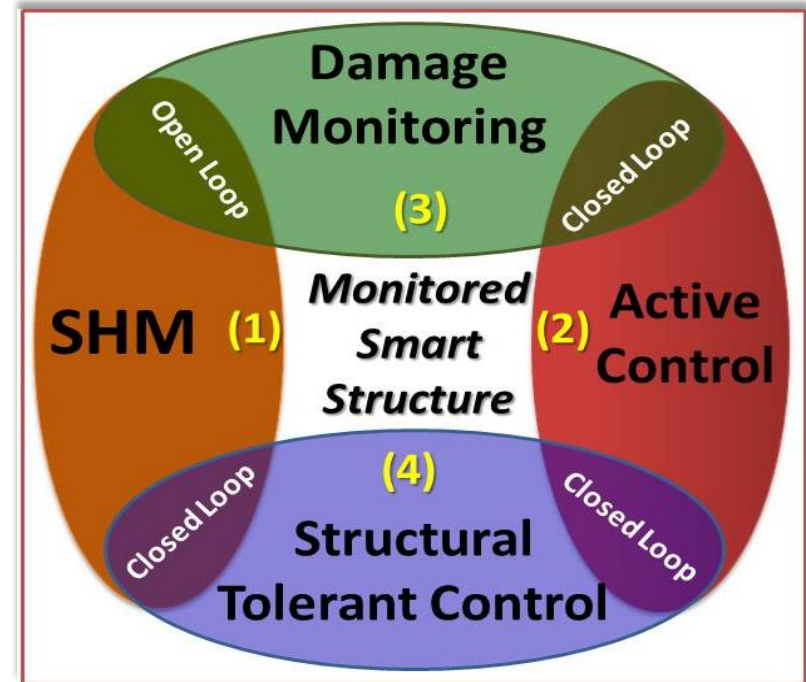
- Introduction and Motivation
- **Damage Tolerant Active Control (DTAC)**
- DTAC strategies: Examples
- Conclusion

✿ Damage Tolerant Active Control – DTAC

- A new paradigm that we have proposed (Mechbal and Nobrega, 2012) to design *fault tolerant controllers*, specifically dedicated to face **structural damages**.
- DTAC makes use of a widely **multidisciplinary** context, which applies knowledge from different fields, such as *mechanical structures modeling*, *signal processing*, *control theory*, fracture mechanics, modal analysis and artificial intelligence, ...

✿ Four principal topics:

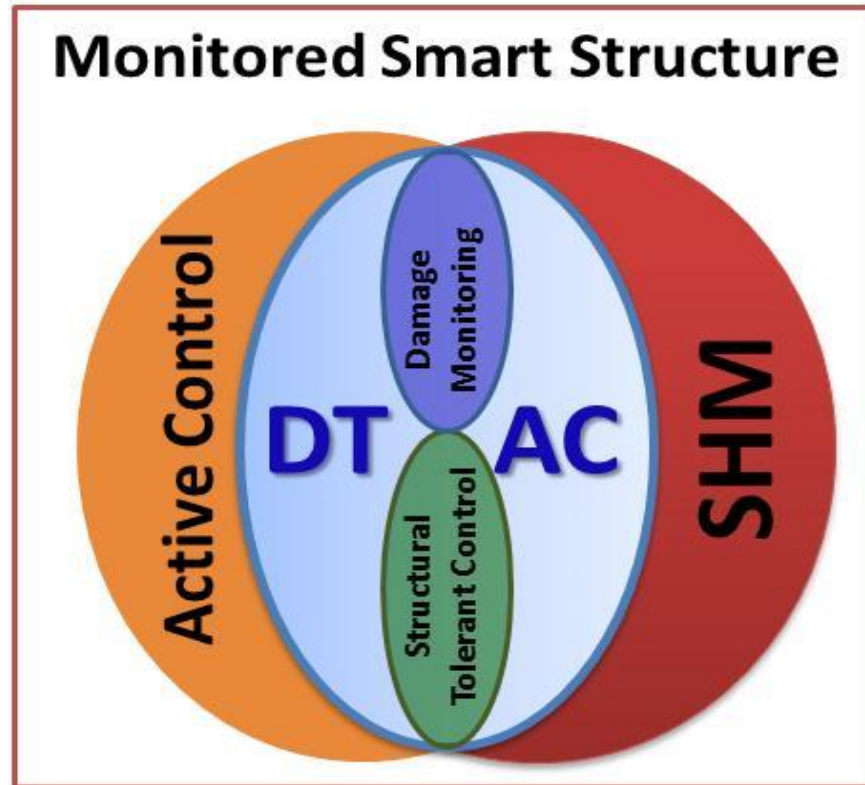
1. *SHM*
2. *Active Control*
3. *Damage Monitoring*
4. *Structural Tolerant Control*



DTAC STRATEGIES

✿ DTAC architectures:

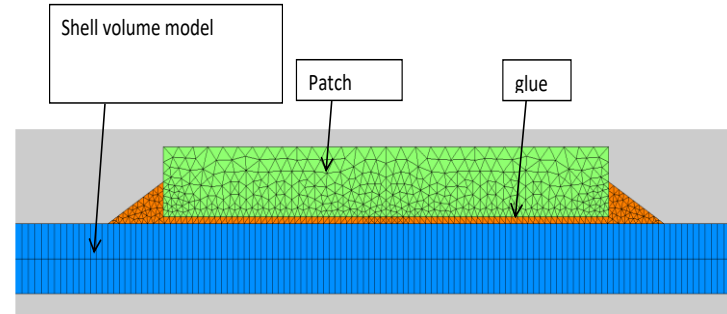
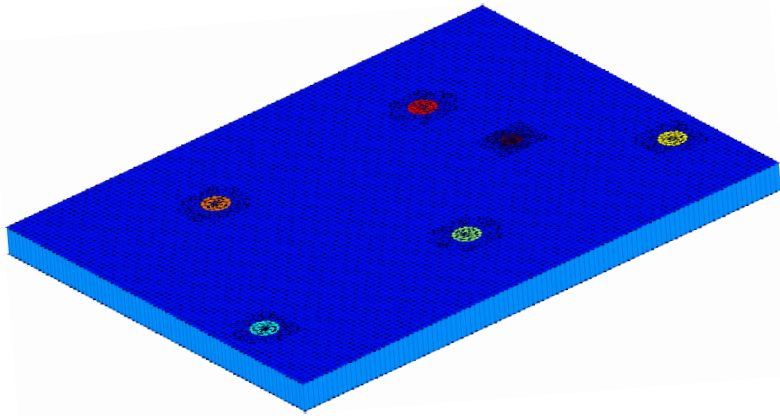
- DTAC combines the functions of **SHM** and **active control**.
- DTAC encompasses two main fields: **damage monitoring** and **damage tolerant control**



DTAC - NUMERICAL SIMULATION

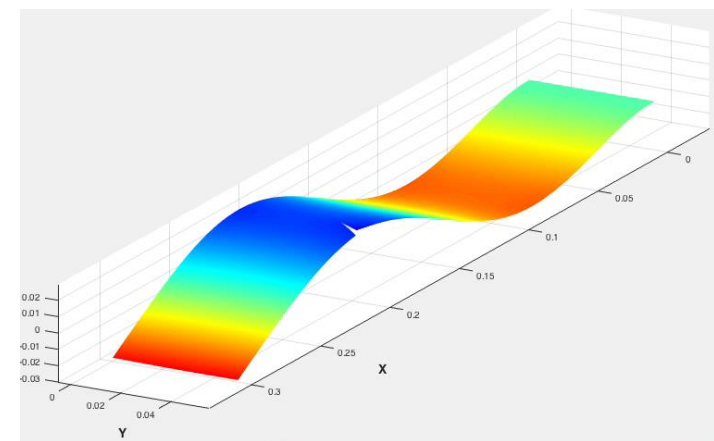
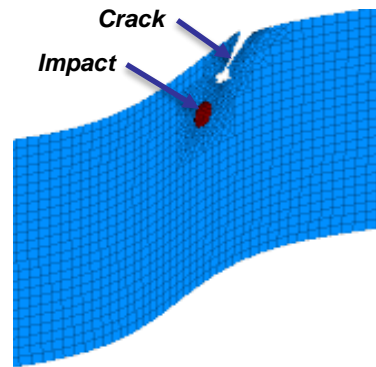
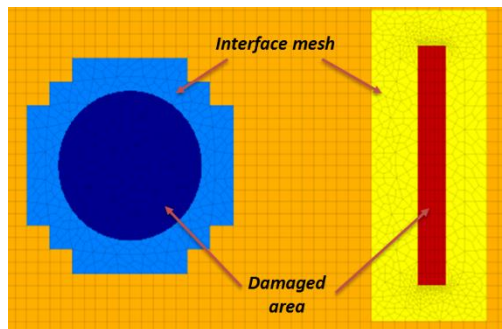
★ Numerical Simulations

➤ Smart Structures with PZT



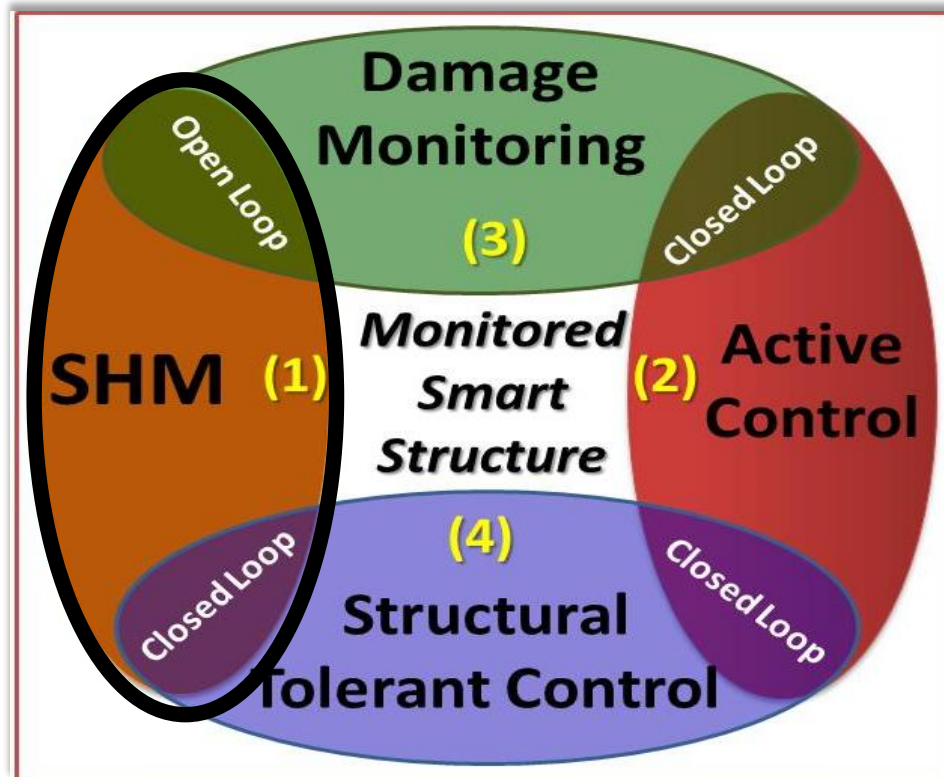
SDT software

➤ and damages



Damage acts as a source in healthy-damaged signal

DTAC TOPICS - SHM



SHM methods

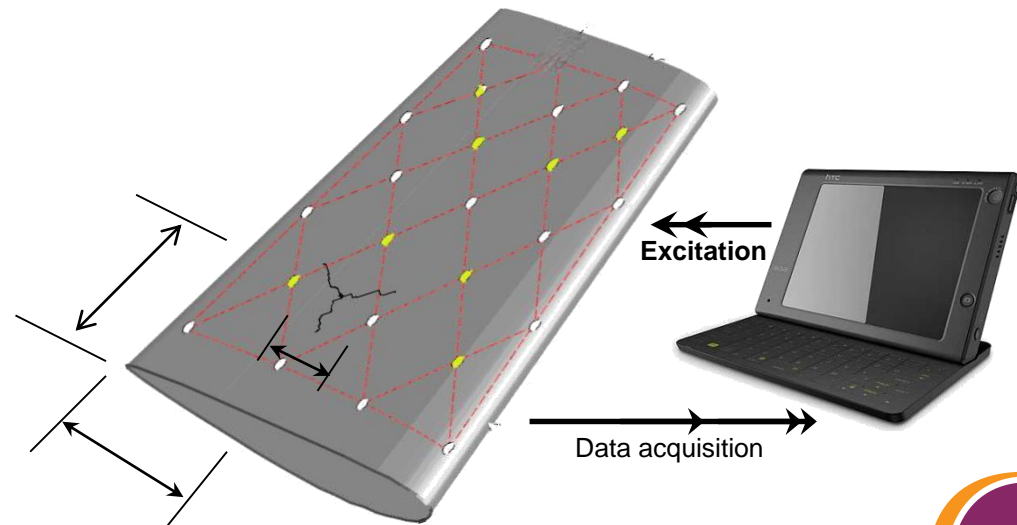
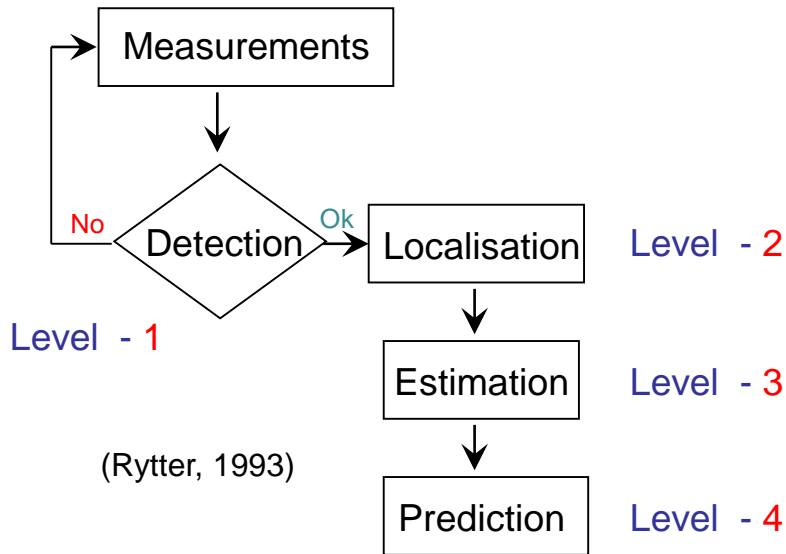
~ Passive Methods~

Use a large number of sensors
Ambient or damaging impacts excitations
Example: *acoustic emission in a loaded structure, output only vibration based approaches*

~ Active Methods~

Possibility to use actuators
Controlled excitations
Example: *acoustic emission emitters and detectors*
– Lamb waves, ...

SHM sequential levels

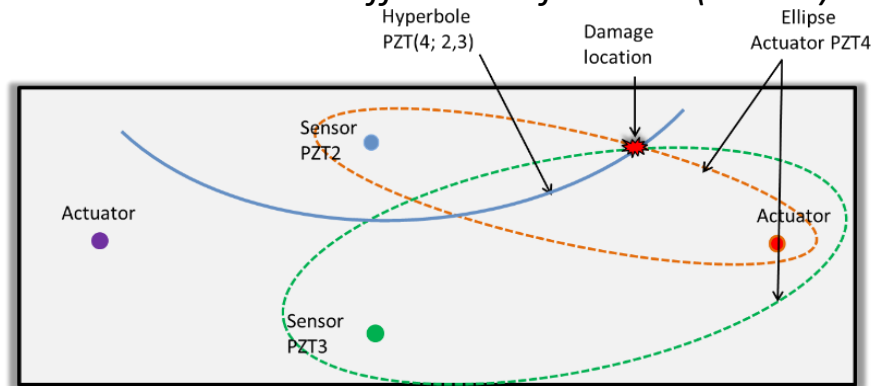


FOCUS: BAYESIAN FRAMEWORK FOR SHM

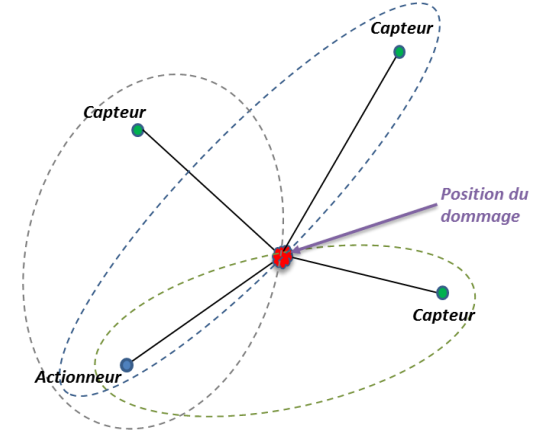
Lamb waves-based damage localization :

➤ Time of flight (Tof) based principle:

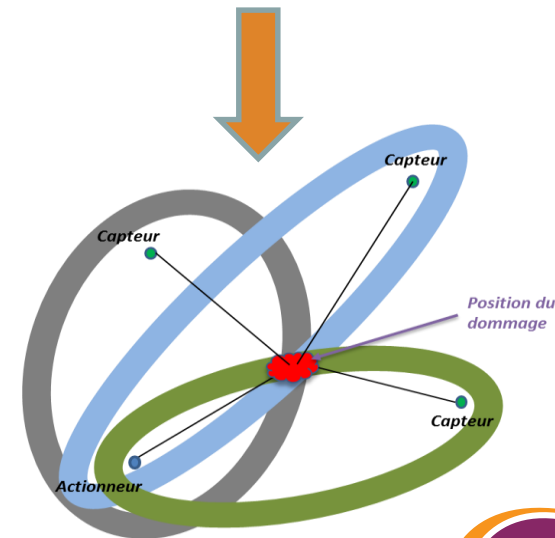
- *Ellipse method*: time of arrival (ToA) :
- *Hyperbola method*: time difference of arrival (TDOAs)



$$d_{a-D} + d_{D-C} = Vg \text{ ToF (scatt. signal)}$$



UNCERTAINTIES

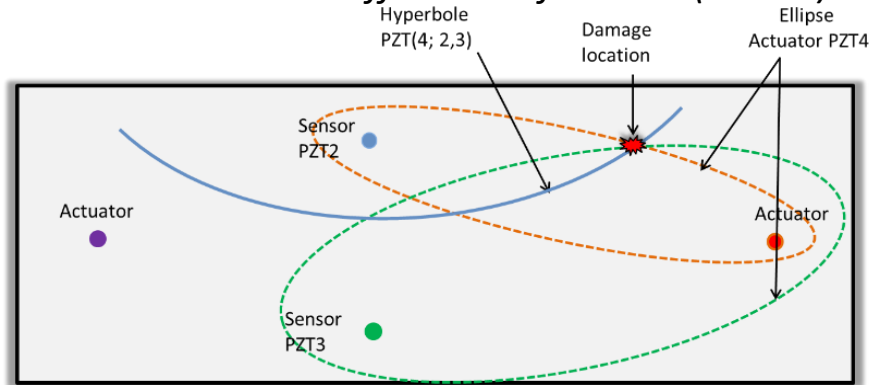


FOCUS: BAYESIAN FRAMEWORK FOR SHM

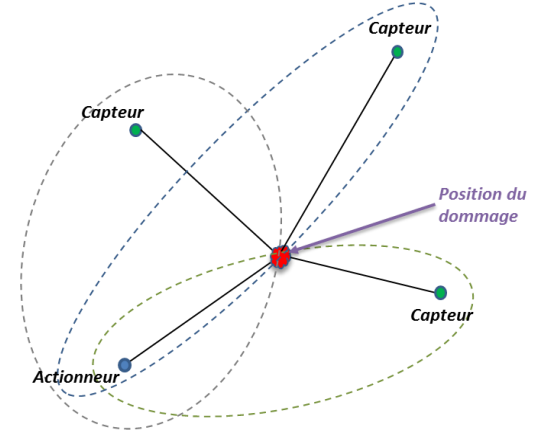
Lamb waves-based damage localization :

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UNCERTAINTIES

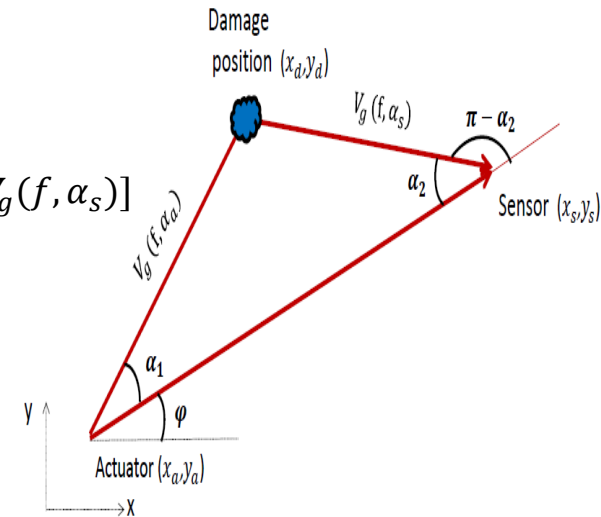
➤ Approach: Bayesian estimation

➤ Bayesian formulation of the *ToF*:

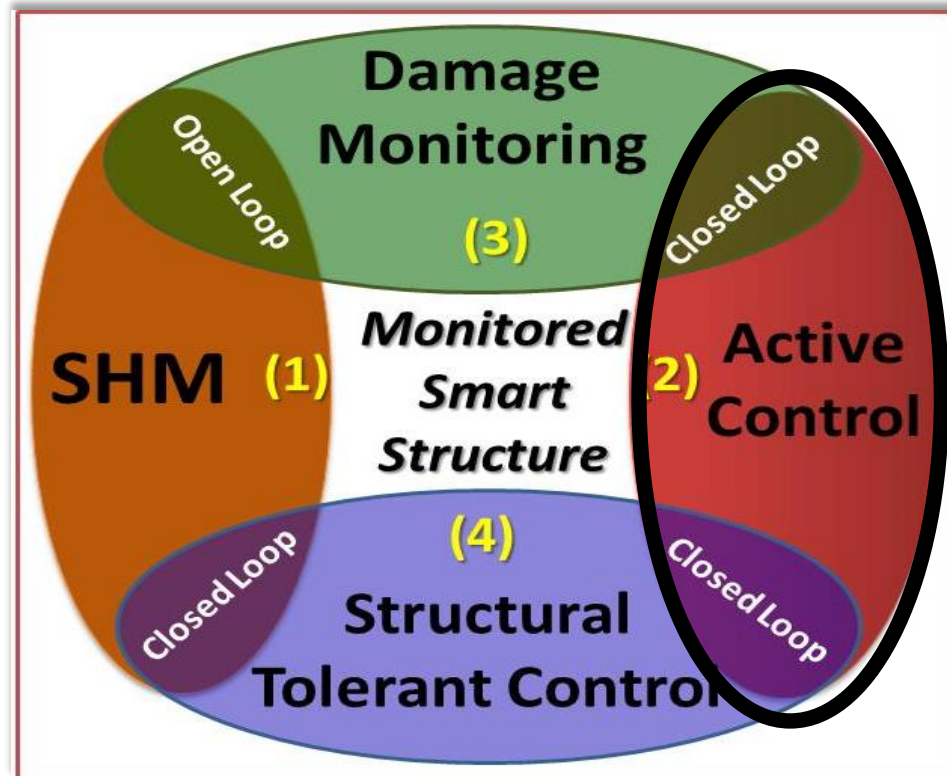
$$\theta = [x_d, y_d, V_g(f, \alpha_a), V_g(f, \alpha_s)]$$

$$Tof_m = Tof_c(\theta) + \varepsilon$$

$$\varepsilon \sim \mathcal{N}(0, \sigma_\varepsilon^2) = \frac{1}{\sigma_\varepsilon \sqrt{2\pi}} \exp\left(-\frac{(Tof_m - Tof_c(\theta))^2}{2\sigma_\varepsilon^2}\right)$$



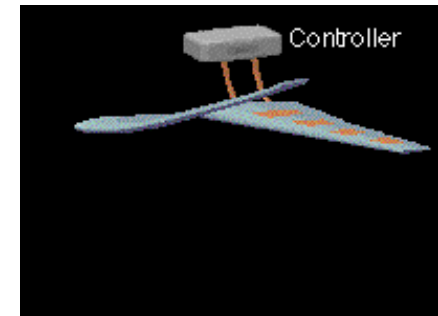
DTAC TOPICS - DAMAGE MONITORING



DTAC TOPICS - ACTIVE CONTROL



- ✿ *Minimize mechanical vibrations of structures preventing from prejudicial damage provoked by excessive strain or by fatigue.*
- ✿ **Control techniques: *feedback* and *feedforward***
 - Modal control avoiding spillover phenomena (Balas, 1978; Inman, 2006)
 - Conventional PID control (Sutton et al., 1999)
 - LQR (Petersen & Pota, 2003) and H_2/H_∞ (Anthonis et al., 1999),
 - Distributed controller (Bhattacharya et al., 2002);
 - Model predictive controller (Wills et al., 2008),
 - Nonlinear controller (Gaudiller et al., 2007);
 - Modal: H_∞ controller (Genari et al., 2014, 2017)
 - A Hybrid controller : H_∞ controller and an adaptive controller (Vergé et al., 2001)
 - Modal H_∞ controller (Genari et al., 2014, 2017)

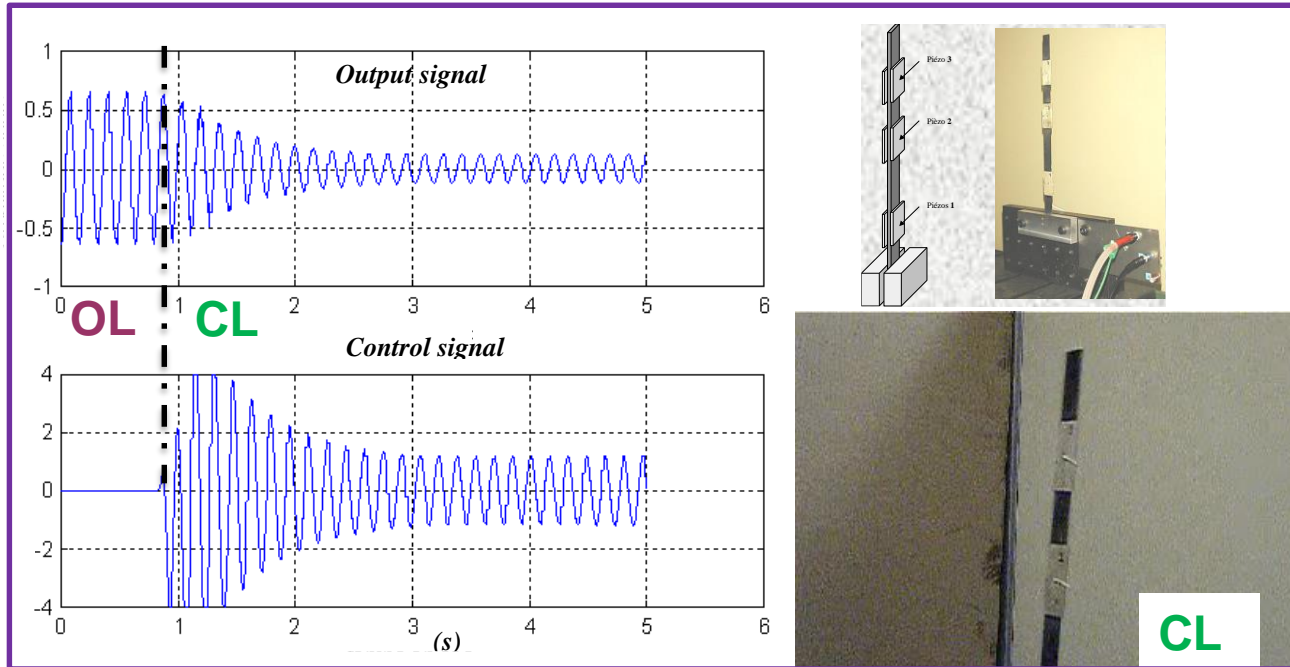


FOCUS : ROBUST H_∞ APPROACH

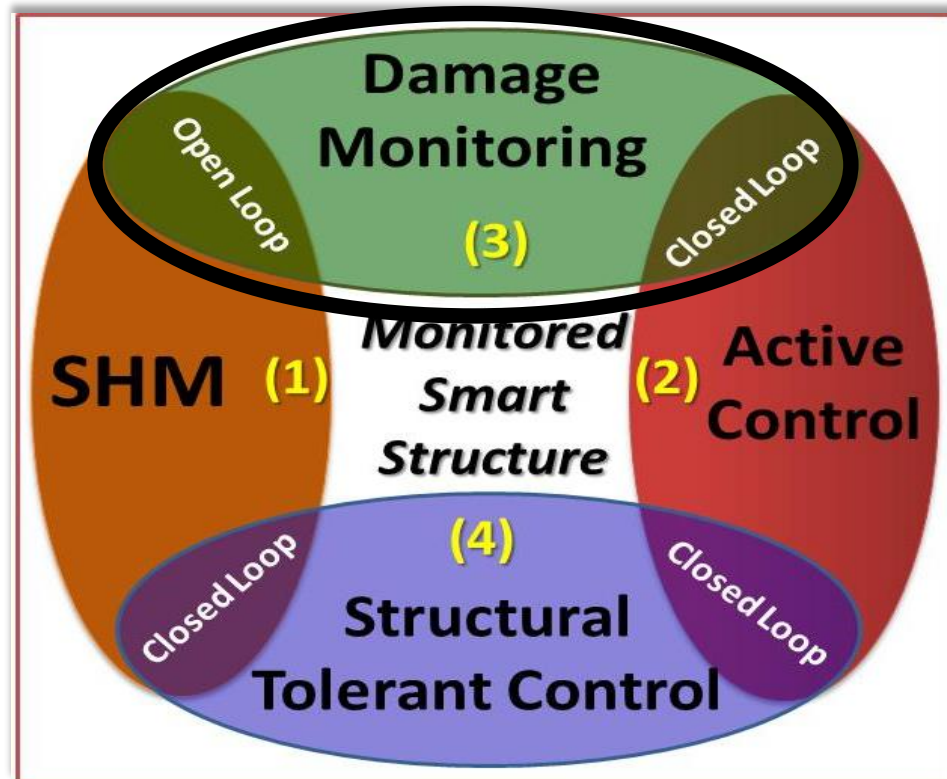


- Robust approaches to disturbance rejection:

Robust H_∞ approach



DTAC TOPICS - DAMAGE MONITORING



✿ Damage monitoring

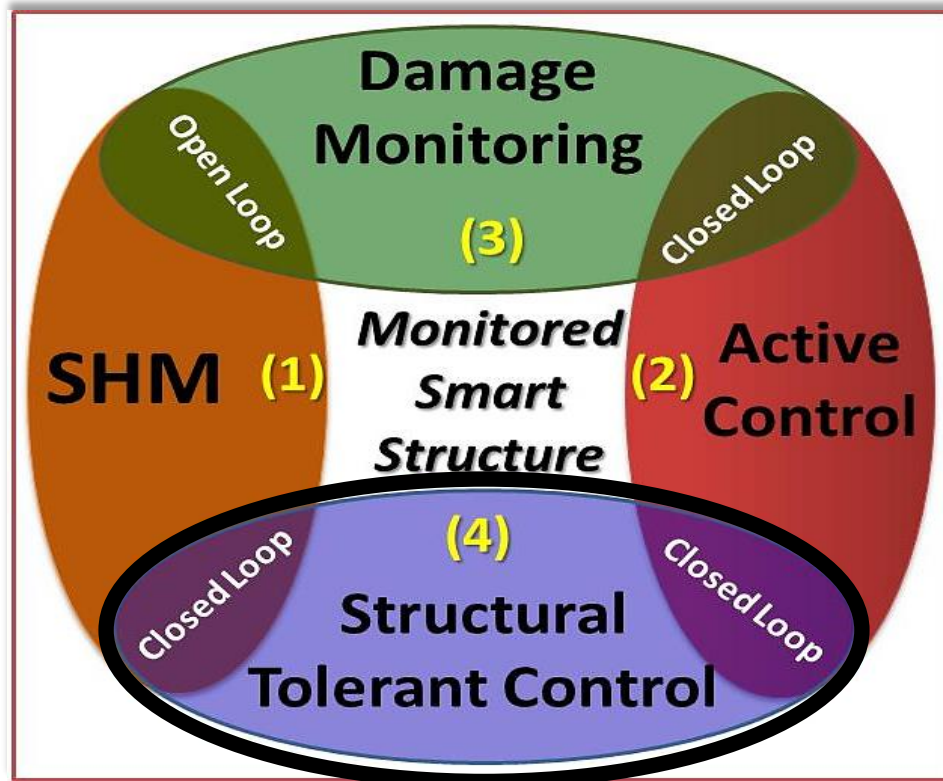
- Monitoring of already *detected* and *localized* damage.
- The goal is to **supervise the evolving** of the damage and to provide **prognosis** about its in-service lifetime.
- It is mainly based on methods described in the SHM area as for example, Lamb wave based approaches and **mechanical/materials** analysis.
- Need to use **models based on fracture mechanics**, **fatigue** life analysis, or structural design assessment.
- It's a transversal area:
 - *book on **prognosis** in SHM (Inman et al., 2005)*
 - *book on **durability** and aging of structures (Pochiraju et al., 2012).*



- ✓ **Durability** of smart structures
- ✓ **Aging Monitoring** with PZT
- ✓ **kinetics of damages.**



DTAC TOPICS - STC





★ Structural tolerant control (STC)

- Deals with the *vibration suppression control problem* against potential damage.
- Provides *satisfactory performances* in terms of vibration rejection under the possible presence of damages
- Simultaneously achieve high performance and structural durability.
- **Approaches:** *robust control and reconfigurable control* (similar to FTC).
- STC could also be used to **monitor** or to **detain** the evolving of damage

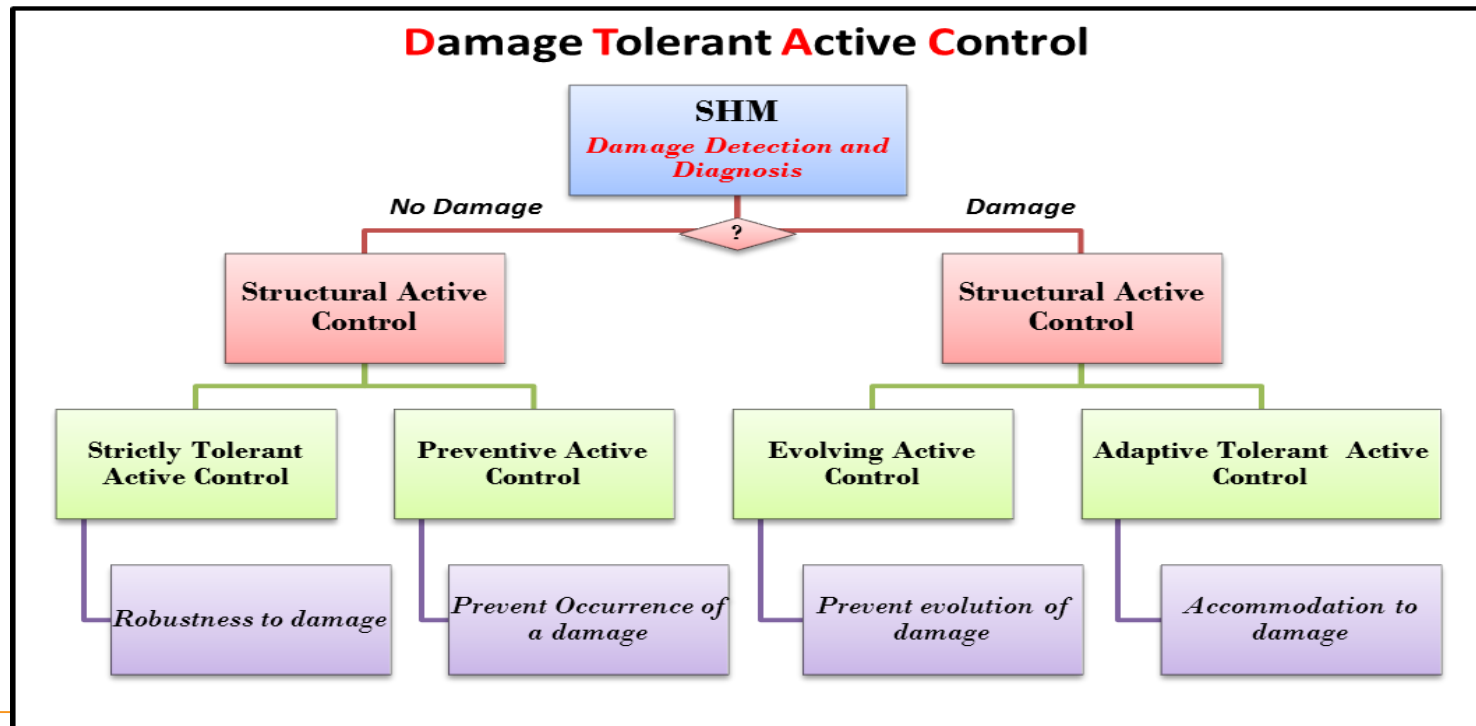
- **However, this subject has seldom been discussed and in the literature, only few works are referred to it (sometimes unwittingly):**
 - The first addressed STC problem: Ahmad et al. (2000) - μ synthesis and H_∞ controllers
 - Caplin et al. (2001): *simultaneously* achieve high performance and **structural durability**.
 - **More recently**, a *damage tolerant LQG modal controller* has been applied to a printed circuit board (PCB) with PZT by (Chomette et al., 2008, 2010).

DTAC STRATEGIES

★ DTAC strategies:

➤ Depending on the objectives and how "smart" is the structure (number, position and type of sensors and actuators), we proposed different ways to perform DTAC:

1. *Strictly Tolerant Active Controller* - **STAC**
2. *Preventive Active Controller* - **PAC**
3. *Evolving Active Controller* - **EAC**
4. *Adaptive Tolerant Active Control* - **ATAC**





✿ Strictly Tolerant Active Controller (STAC)

- **Fixed** and **robust** enough to guarantee a minimal **acceptable performance** to some **future damage** level.
- *The compromise between robustness and performance may conduct to a **poor** controller behavior for **a not damaged** structure*

✿ Preventive Active Controller (PAC)

- **Avoid** or **delay the occurrence** of damages
- This is the **aim of several recent works**. (Chomette et al., 2010).

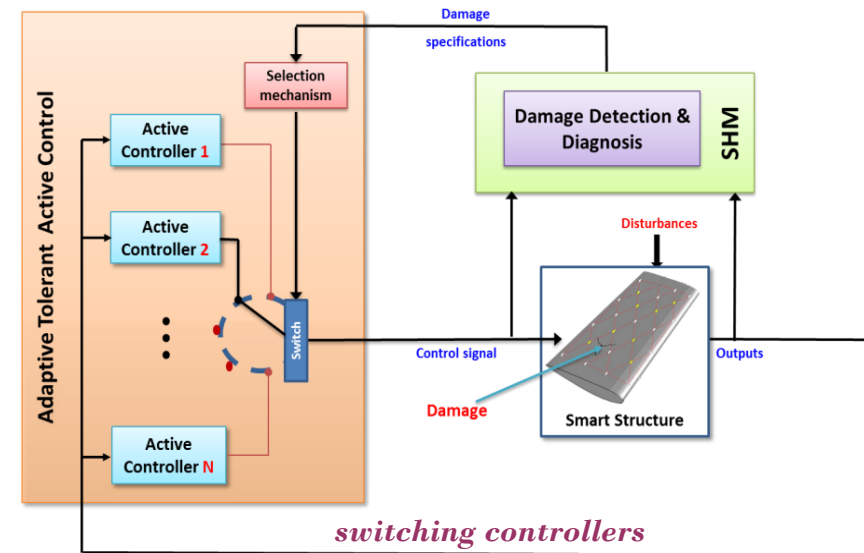
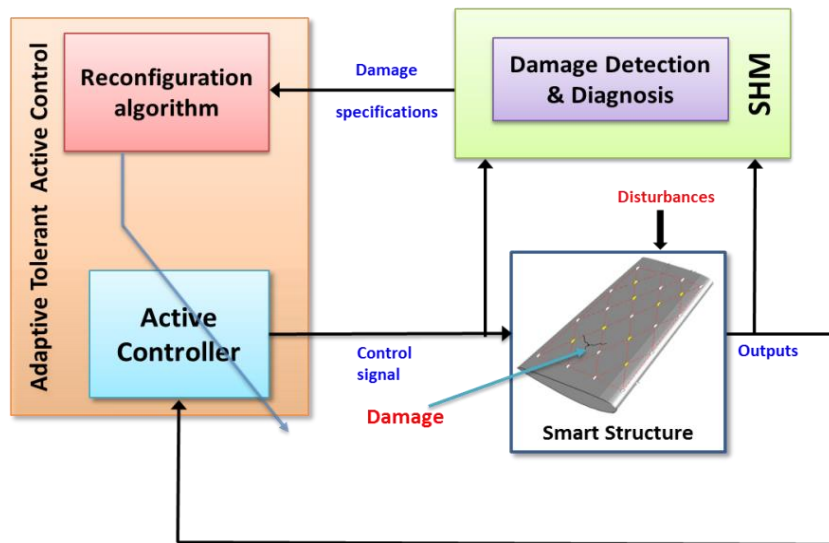
✿ Evolving Active Controller (EAC)

- **Protect** the structure avoiding the **evolution** of the damage.
- Achieve vibration reduction and perform **damage prognosis**

✿ Adaptive Tolerant Active Control (ATAC)

- **Accommodate** a detected damage.
- Include an **SHM module**
- Different system configurations are possible:

DTAC STRATEGIES



✿ Adaptive Tolerant Active Control (ATAC)

- Accommodate a detected damage.
- Include an **SHM module**
- Different system configurations are possible:



✿ The goals:

- To control the vibration in predefined **regions** of the structure,
- To perform **self diagnosis** and to accommodate for damages
- To adapt automatically the **control spatially** when a damage occurs
- To pay attention to the number of active elements

✿ Problems:

- The **spatial dimension**
 - *what's about vibration reduction over the entire structure ?*
- The curse of dimensionality ! → Model **reduction** problems
- The interaction between the **SHM** and the control systems is not straightforward
 - **Stability** issues
- It's a **Singular Perturbation** control problem – two dynamics !
- **Numerical** simulations and experimentations



✿ To deal with such problems:

- Robust control
- Adaptive control
- Distributed and decentralized approach
- FTC methods

✿ Two approaches:

- Adaptive Modal H_∞ control & Subspace metric for damage monitoring (Genari, et al., 2015, 2017)
- Spatial H_2/H_∞ control (Mechbal and Nobrega, 2014, 2015)



- Introduction and Motivation
- Damage Tolerant Active Control (DTAC)
- **DTAC Strategies & Examples**
- Conclusion

★ Modal H_∞ Control Problem

- According to the optimal controller design framework, a performance indicator is introduced as an output vector $\mathbf{z}(t)$, leading to the following state-space equations:

$$\begin{aligned}\dot{\mathbf{x}}(t) &= \mathbf{A}\mathbf{x}(t) + \mathbf{B}_1\mathbf{w}(t) + \mathbf{B}_2\mathbf{u}(t) \\ \mathbf{z}(t) &= \mathbf{C}_1\mathbf{x}(t) + \mathbf{D}_{11}\mathbf{w}(t) + \mathbf{D}_{12}\mathbf{u}(t) \\ \mathbf{y}(t) &= \mathbf{C}_2\mathbf{x}(t) + \mathbf{D}_{21}\mathbf{w}(t) + \mathbf{D}_{22}\mathbf{u}(t),\end{aligned}\quad (4)$$

in which the matrices \mathbf{C}_1 , \mathbf{D}_{11} , and \mathbf{D}_{12} are chosen to define the desired performance vector.

- The H_∞ control problem is to find a controller \mathbf{K}_c to the plant given by Eq. (4), if there is one, stated as:

$$\begin{aligned}\dot{\mathbf{x}}_c(t) &= \mathbf{A}_c\mathbf{x}_c(t) + \mathbf{B}_c\mathbf{y}(t) \\ \mathbf{u}(t) &= \mathbf{C}_c\mathbf{x}_c(t) + \mathbf{D}_c\mathbf{y}(t),\end{aligned}\quad (5)$$

such that, for the closed-loop system and given a $\gamma > 0$,

$$\underbrace{\inf}_{\mathbf{K}_c \in V} \underbrace{\sup}_{\mathbf{w} \neq 0, \mathbf{w} \in \mathcal{L}_2[0, \infty)} \frac{\int_0^\infty \mathbf{z}^T(t)\mathbf{z}(t)dt}{\int_0^\infty \mathbf{w}^T(t)\mathbf{w}(t)dt} < \gamma^2,$$

in which V represents the set of all controllers that stabilises the plant.

FOCUS: MODAL H_∞ CONTROLLER - STAC

★ Modal H_∞ Control problem

Theorem (Modal H_∞ theorem)

Consider the H_∞ problem of designing a controller \mathbf{K}_c given in Eq. (5) for a structure according to Eq. (4) with the modal state matrix according to Eq. (2) and the following performance output:

$$\mathbf{z}_p(t) = \mathbf{\Gamma}\mathbf{x}(t) + \mathbf{\Theta}\mathbf{w}(t) + \mathbf{\Lambda}\mathbf{u}(t), \quad (6)$$

with

$$\mathbf{\Gamma} = \begin{bmatrix} \mathbf{Q}_1^{\frac{1}{2}}\mathbf{C}_{1_1} & \mathbf{Q}_2^{\frac{1}{2}}\mathbf{C}_{1_2} & \cdots & \mathbf{Q}_m^{\frac{1}{2}}\mathbf{C}_{1_m} \end{bmatrix}, \quad \mathbf{\Theta} = (\mathbf{Q}_1^{\frac{1}{2}}\mathbf{D}_{11_1} + \cdots + \mathbf{Q}_m^{\frac{1}{2}}\mathbf{D}_{11_m}),$$
$$\mathbf{\Lambda} = (\mathbf{Q}_1^{\frac{1}{2}}\mathbf{D}_{12_1} + \cdots + \mathbf{Q}_m^{\frac{1}{2}}\mathbf{D}_{12_m}),$$

where the diagonal matrix $\mathbf{Q}_i > 0$ weights mode i and \mathbf{C}_{1_i} , \mathbf{D}_{11_i} , and \mathbf{D}_{12_i} correspond to the respective mode i submatrices in \mathbf{C}_1 , \mathbf{D}_{11} , and \mathbf{D}_{12} .

Then, given a scalar $\gamma > 0$, a controller that solves the respective H_∞ problem:

$$\|\mathbf{T}_{z_p w}(s)\|_\infty < \gamma,$$

also guarantees that:

$$\|\mathbf{T}_{z w}(s)\|_{\infty, \mathbf{Q}} < \gamma,$$

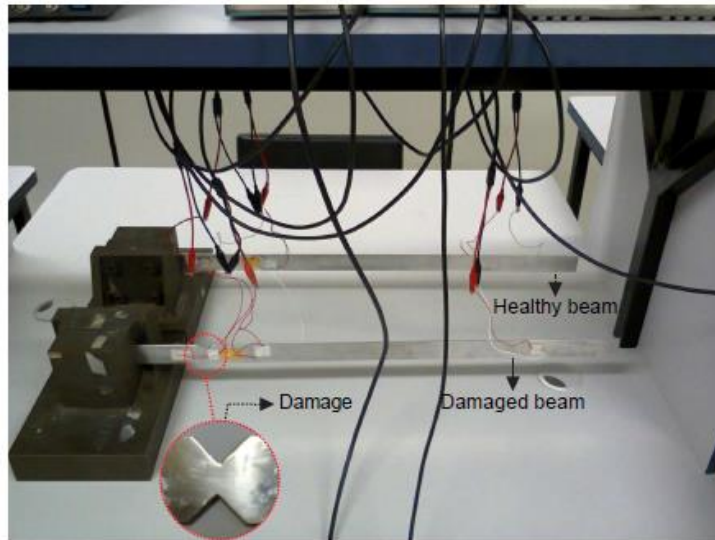
where $\mathbf{T}_{z_p w}(s)$ and $\mathbf{T}_{z w}(s)$ are the closed-loop transfer matrices using \mathbf{K}_c for the modal performance vectors.

FOCUS: MODAL H_∞ CONTROLLER - STAC

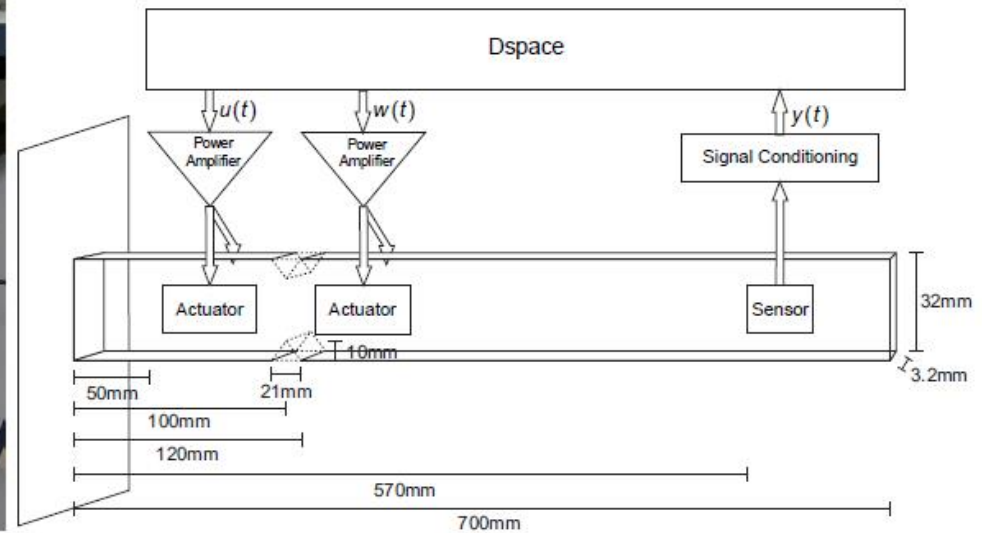
Experiment results

Objectives:

- Test the methodology for the **regular active vibration control**;
- Test the methodology for DTAC using the **STAC strategy**;



(a) Aluminium beams.



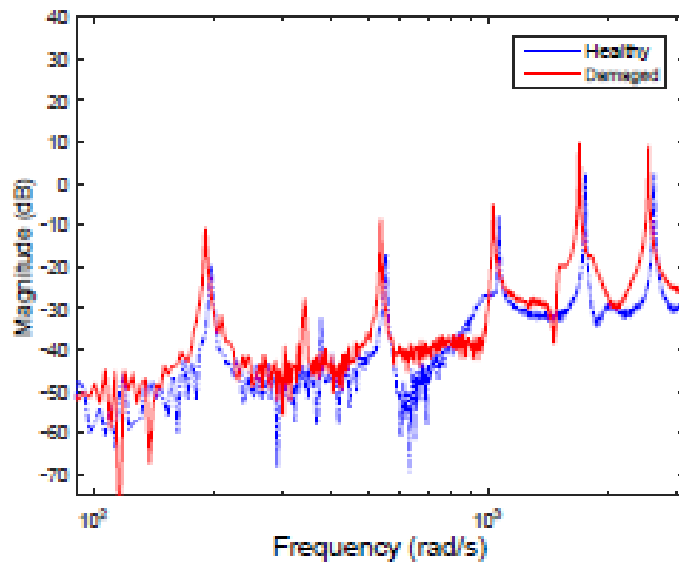
(b) Block diagram.

FOCUS: MODAL H_∞ CONTROLLER - STAC

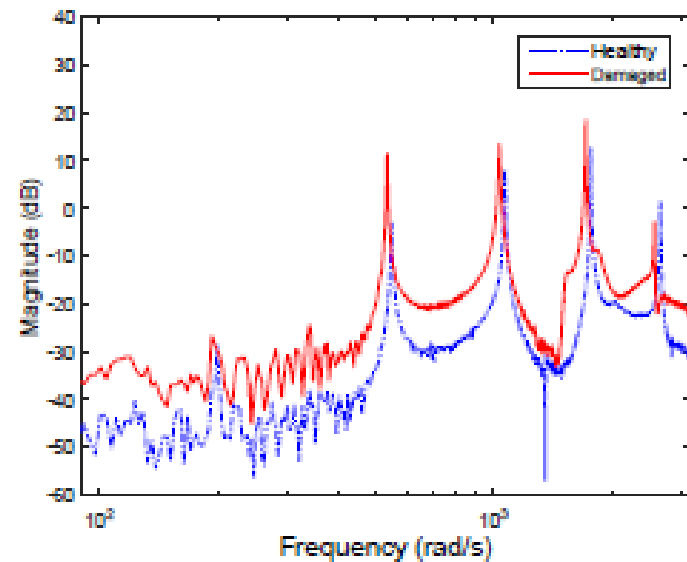


✿ Experiment results

- Application of the controller for the **healthy** and **damaged structure**;
- Frequency response comparison between the healthy and the damaged structures:



(a) P_{yu} .

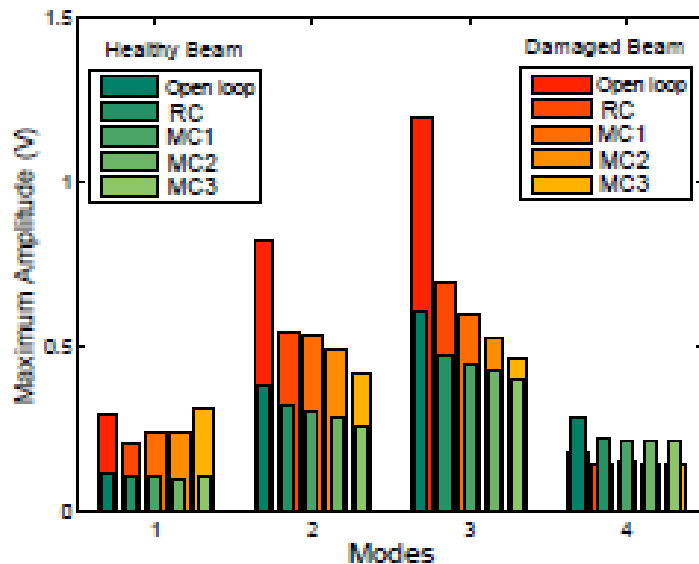


(b) P_{yw} .

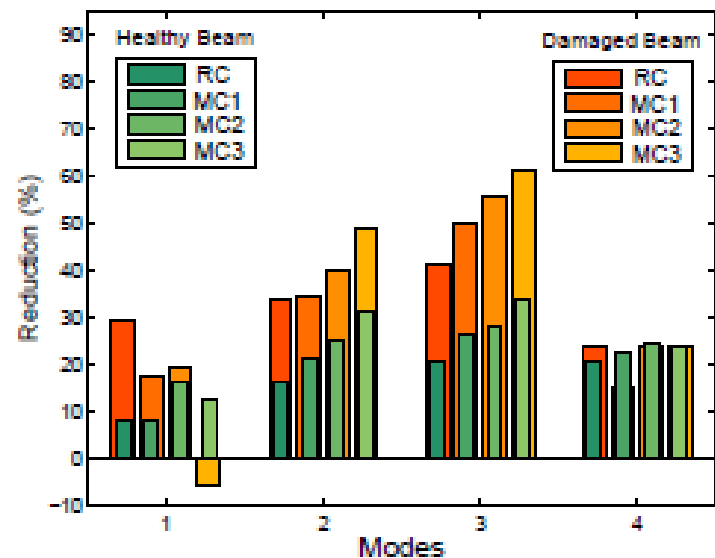
FOCUS: MODAL H_∞ CONTROLLER - STAC

✳ Experiment results

- Application of the controller for the **healthy** and **damaged structure**;
- The **weighing** increase leads to **vibration reduction** for the healthy and the damaged structures;

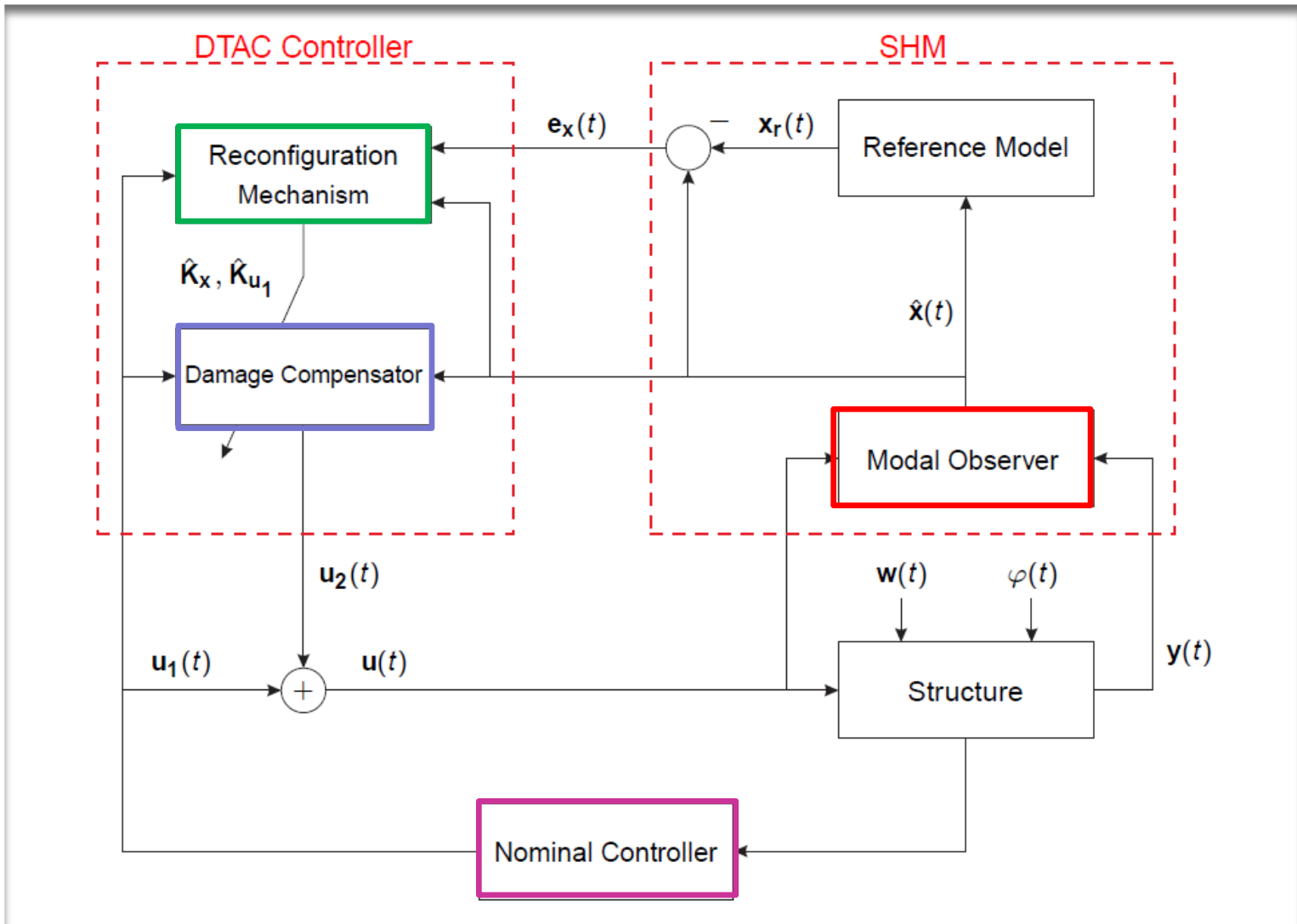


(a) Peak vibration of each mode.



(b) Percentage reduction.

Modal Double-Loop Framework



Reconfiguration mechanism

Theorem

The state-tracking error dynamics given in Eq. (10) are stable for the following adaptive gain laws:

$$\dot{\hat{\mathbf{K}}}_{\mathbf{x}}(t) = -\mathbf{T}_{\mathbf{x}}\hat{\mathbf{x}}(t)\mathbf{e}_{\mathbf{x}}^T(t)\mathbf{P}\mathbf{B}_2, \quad (12)$$

$$\dot{\hat{\mathbf{K}}}_{\mathbf{u}_1}(t) = -\mathbf{T}_{\mathbf{u}_1}\mathbf{u}_1(t)\mathbf{e}_{\mathbf{x}}^T(t)\mathbf{P}\mathbf{B}_2, \quad (13)$$

in which for $\mathbf{R} = \mathbf{R}^T > 0$, $\mathbf{P} = \mathbf{P}^T > 0$ satisfies the following algebraic Lyapunov equation:

$$\mathbf{P}\mathbf{A}_r + \mathbf{A}_r^T\mathbf{P} = -\mathbf{R}. \quad (14)$$

Moreover, $\mathbf{T}_{\mathbf{x}} > 0$ and $\mathbf{T}_{\mathbf{u}_1} > 0$ are diagonal matrices that determine adaptation rates. Matrix $\mathbf{T}_{\mathbf{x}}$ is a function of the modal adaptation-rate submatrices:

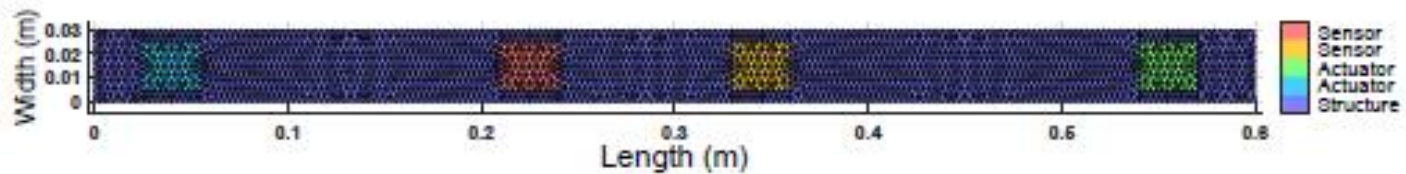
$$\mathbf{T}_{\mathbf{x}} = \begin{bmatrix} \mathbf{T}_1 & \mathbf{0} & \cdots & \mathbf{0} \\ \mathbf{0} & \mathbf{T}_2 & \cdots & \mathbf{0} \\ \vdots & \vdots & \ddots & \vdots \\ \mathbf{0} & \mathbf{0} & \mathbf{0} & \mathbf{T}_m \end{bmatrix}, \quad (15)$$

where the 2×2 matrix \mathbf{T}_i determines the adaptation rate of mode i .

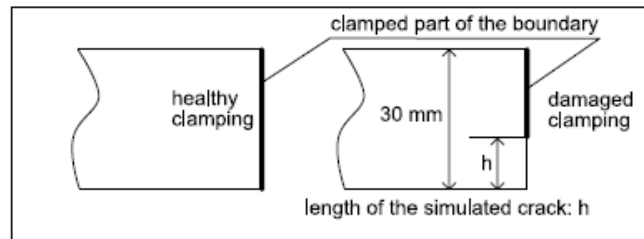
FOCUS: MODAL DOUBLE-LOOP - PAC



FE Simulations:



- Damage 2: $h = 15$ mm;
- Damage 3: $h = 20$ mm.

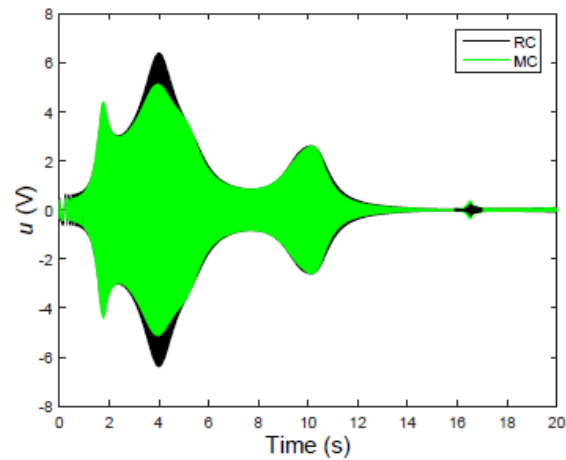
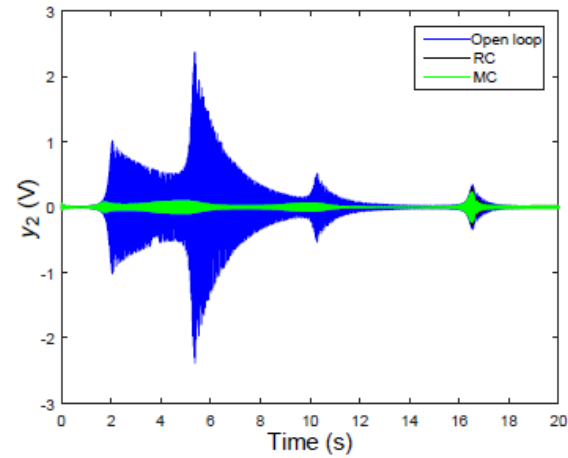
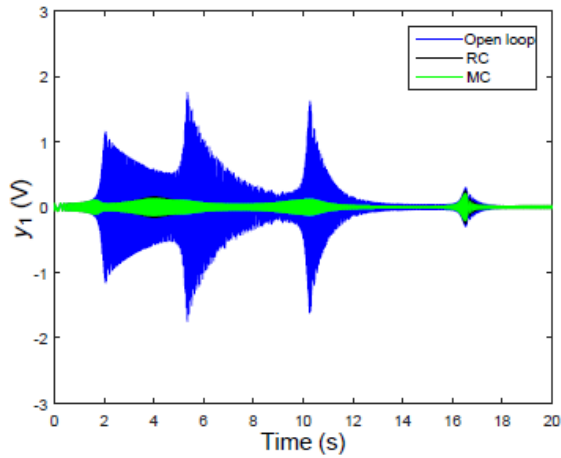


- The **chirp** signal of the previous examples is used as **disturbance**, considering **three cycles of 12 repetitions**;
- **For each cycle**, there is **one condition** of the structure: healthy or damage 2, or damage 3;

FOCUS: MODAL DOUBLE-LOOP - PAC



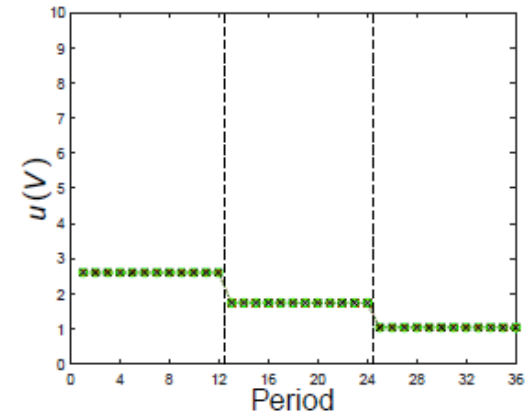
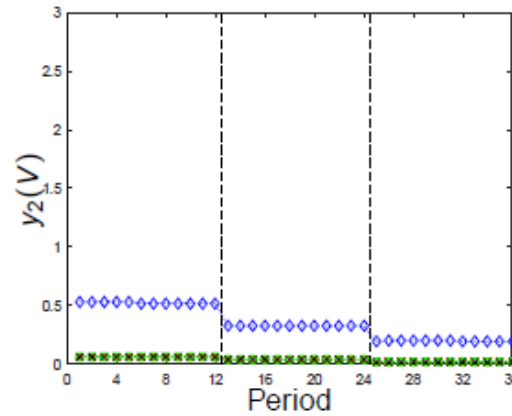
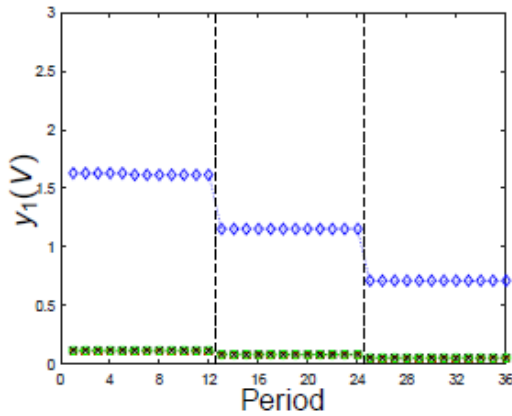
Results: Healthy structure



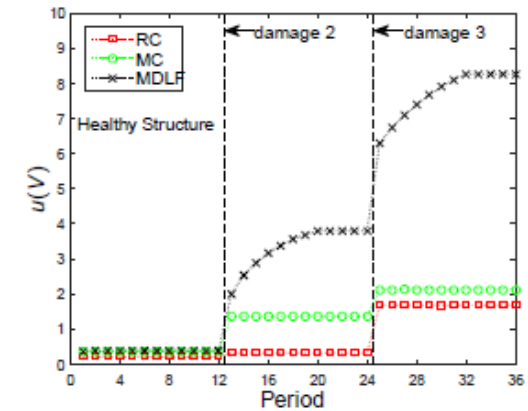
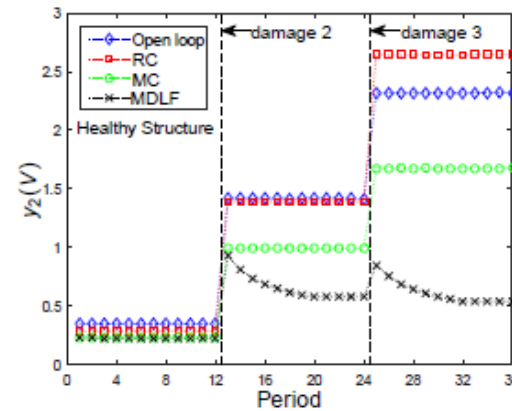
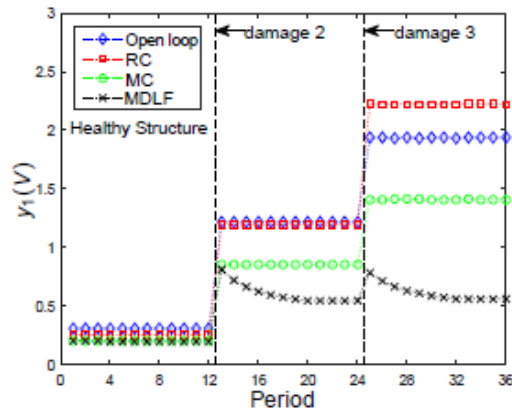
FOCUS: MODAL DOUBLE-LOOP - PAC



Results: Damage Controller



(a) Mode 3.



(b) Mode 4.

FOCUS: A SPATIAL H_∞ CONTROL APPROACH

★ H_∞ controller

➤ Time dependence formulation:

$$\dot{x}_p(t) = A_p x_p(t) + B_w w(t) + B_u u(t)$$

$$z(t) = C_z x_p(t) + D_{zw} w(t) + D_{zu} u(t)$$

$$y(t) = C_y x_p(t) + D_{yw} w(t)$$

➤ Controller K ,

$$\dot{x}_k(t) = A_k x_k(t) + B_k y(t)$$

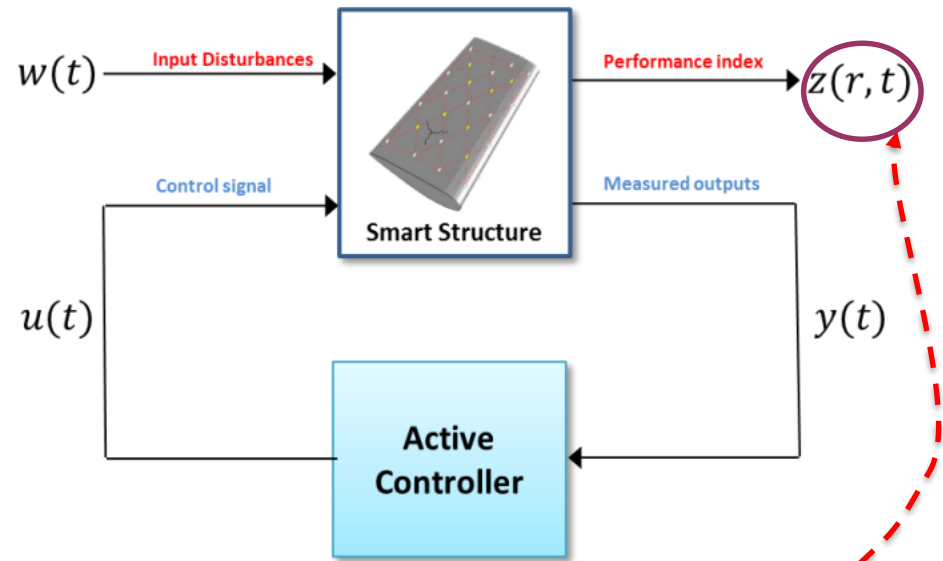
$$u(t) = C_k x_k(t) + D_k y(t)$$

➤ Criterion

$$\sup_{w \in L_2[0, \infty)} J_\infty < \gamma^2$$

$$\|G(s)\|_\infty = \sup_{\omega} \sigma_{\max}(G(j\omega))$$

$$J_\infty = \frac{\|z(t)\|_2^2}{\|w(t)\|_2^2} = \frac{\int_0^\infty z(t)^T z(t) dt}{\int_0^\infty w(t)^T w(t) dt}$$



Problem: How to conveniently incorporate the spatial information of the of structure ?

FOCUS: A SPATIAL H_∞ CONTROL APPROACH

★ H_∞ controller

➤ Time dependence formulation:

$$\begin{cases} \dot{x}_p(t) = A_p x_p(t) + B_w w(t) + B_u u(t) \\ z(t, \mathbf{r}) = C_z(\mathbf{r}) x_p(t) + D_{zw}(\mathbf{r}) w(t) + D_{zu}(\mathbf{r}) u(t) \\ y(t) = C_y x_p(t) + D_{yw} w(t) \end{cases}$$

➤ Controller K ,

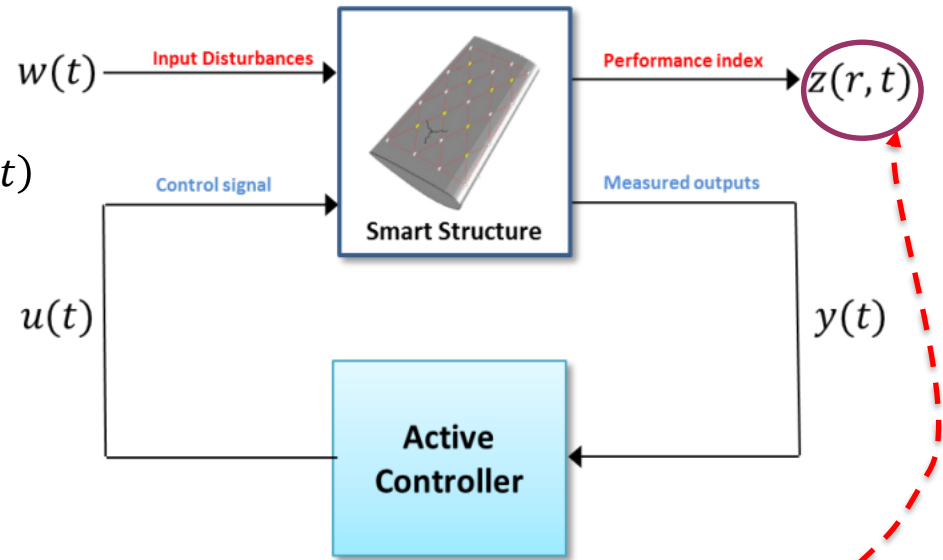
$$\begin{aligned} \dot{x}_k(t) &= A_k x_k(t) + B_k y(t) \\ u(t) &= C_k x_k(t) + D_k y(t) \end{aligned}$$

➤ Criterion

$$\sup_{w \in L_2[0, \infty)} J_\infty < \gamma^2$$

$$\|G(s)\|_\infty = \sup_{\omega} \sigma_{\max}(G(j\omega))$$

$$J_\infty = \frac{\|z(t)\|_2^2}{\|w(t)\|_2^2} = \frac{\int_0^\infty z(t)^T z(t) dt}{\int_0^\infty w(t)^T w(t) dt}$$



Problem: How to conveniently incorporate the spatial information of the of structure ?

FOCUS: A SPATIAL H_∞ CONTROL APPROACH

★ Spatial H_∞ controller:

- Use spatial norms:

$$\|G(s, r)\|_\infty^2 = \sup \lambda_{\max} \left(\int_{\Omega} G^*(j\omega, r) G(j\omega, r) dr \right)$$

- which guarantees **average reduction** of vibration throughout the **entire** structure
- **For specific region Ω** where we want to minimize the H_∞ spatial norm, a space dependent weighing matrix $Q(r)$, where r is the spatial vector, is introduced:

$$J_\infty = \frac{\int_0^\infty \int_{\Omega} z(t, r)^T Q(r) z(t, r) dr dt}{\int_0^\infty w(t)^T w(t) dt}$$

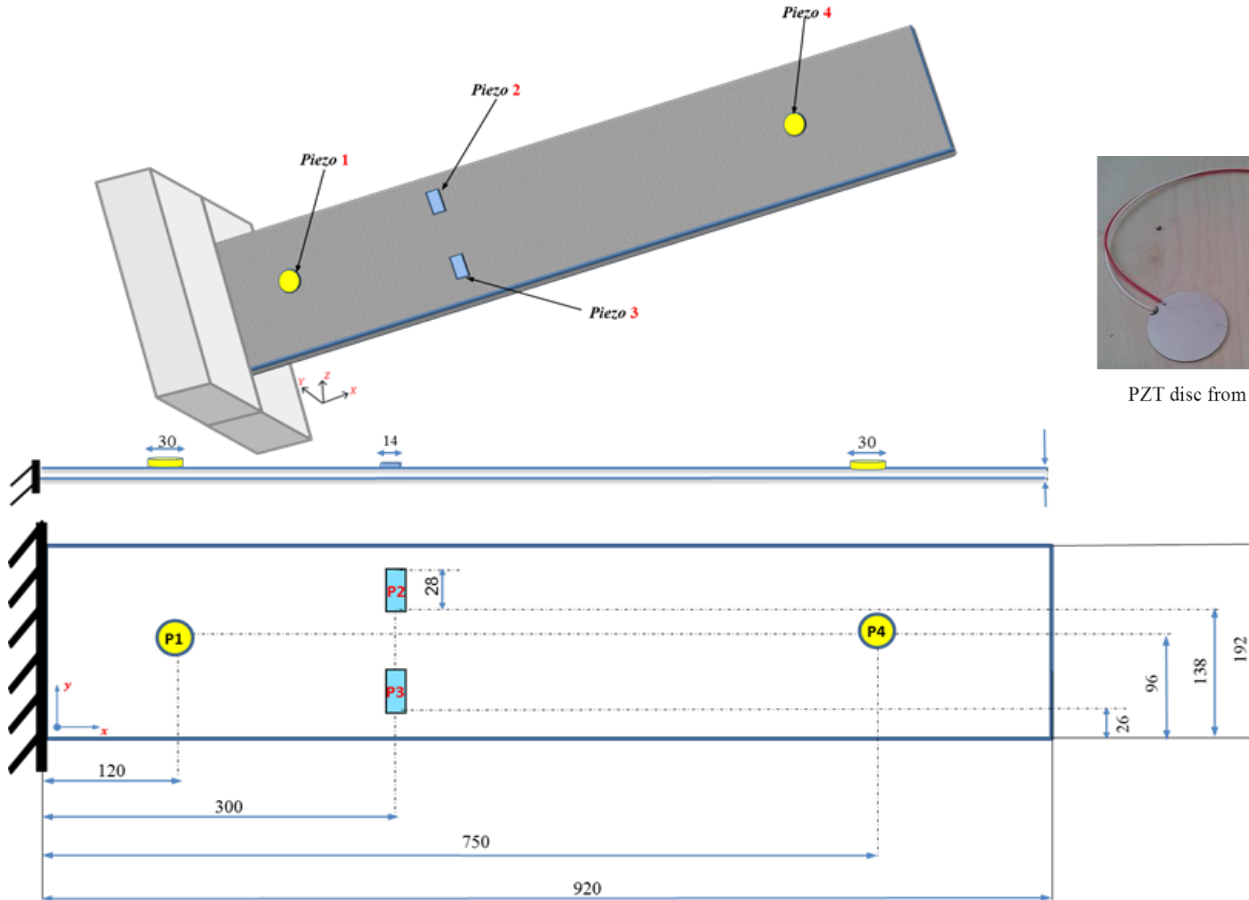
- New performance index output vector with space dependence is driven:

$$z(t, r) = C_z(r)x_p(t) + D_{zw}(r)w(t) + D_{zu}(r)u(t)$$

DTAC – AN EXAMPLE

★ An example: Cantilevered active composite structure

Plate like-beam: 4 epoxy/carbon layers with orientation $[0^\circ/-45^\circ/+45^\circ/0^\circ]$.



PZT disc from NOLIAC

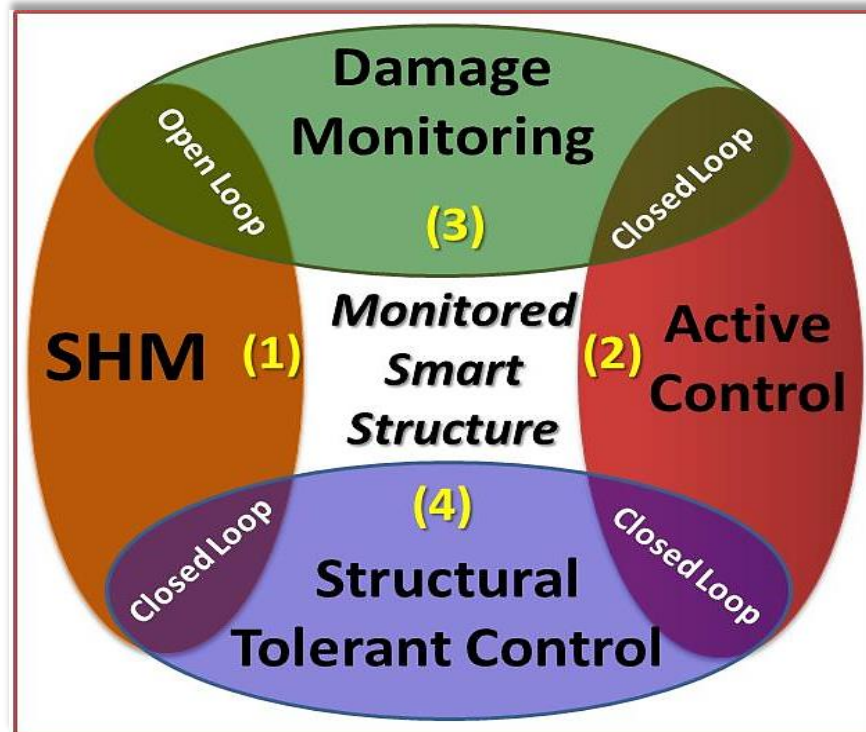


MFC patch from SMART-MATERIALS

DTAC – AN EXAMPLE

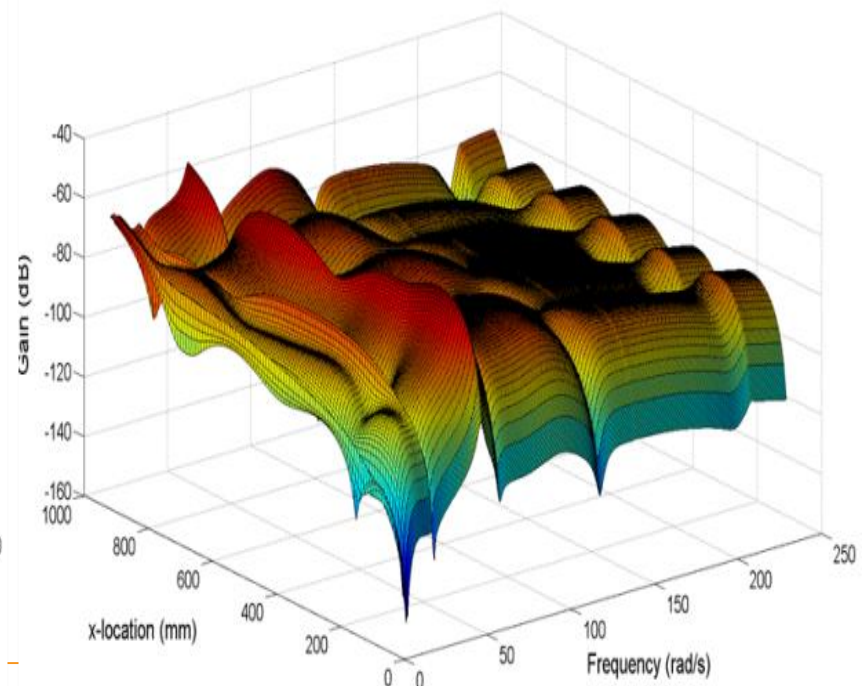
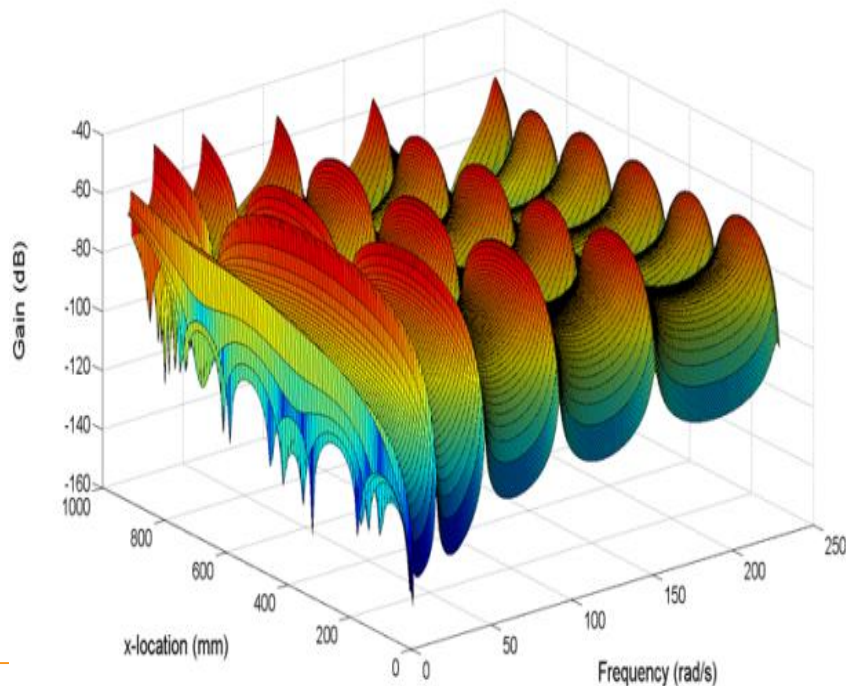
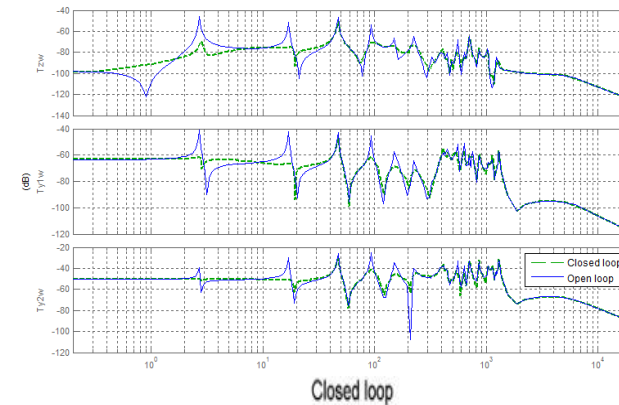
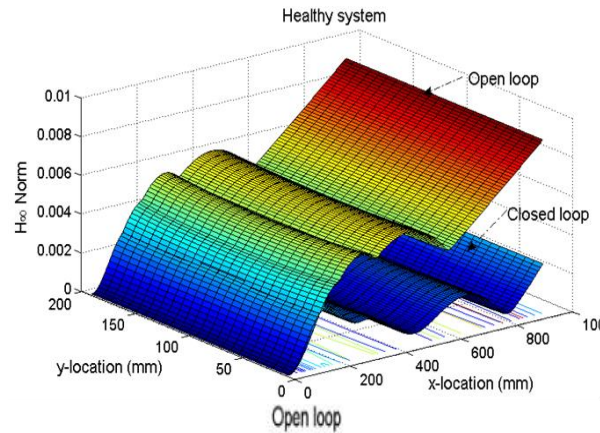
✿ An example: Cantilevered active composite structure

- Robust controller
- Reconfigurable controller
- Evolving controller



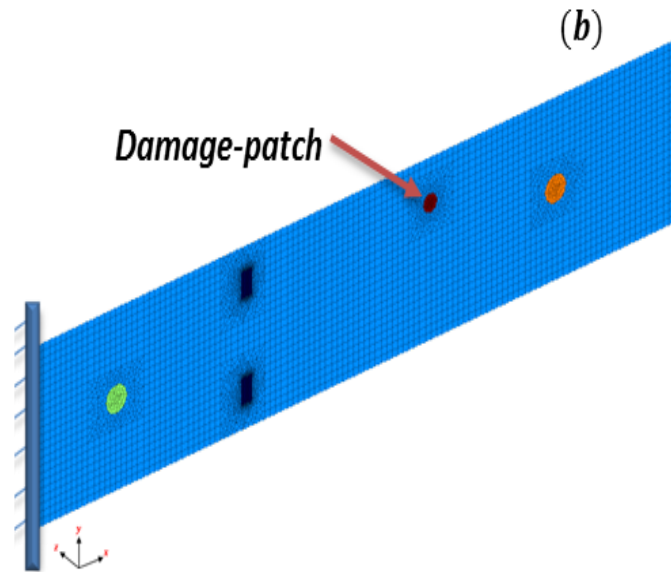
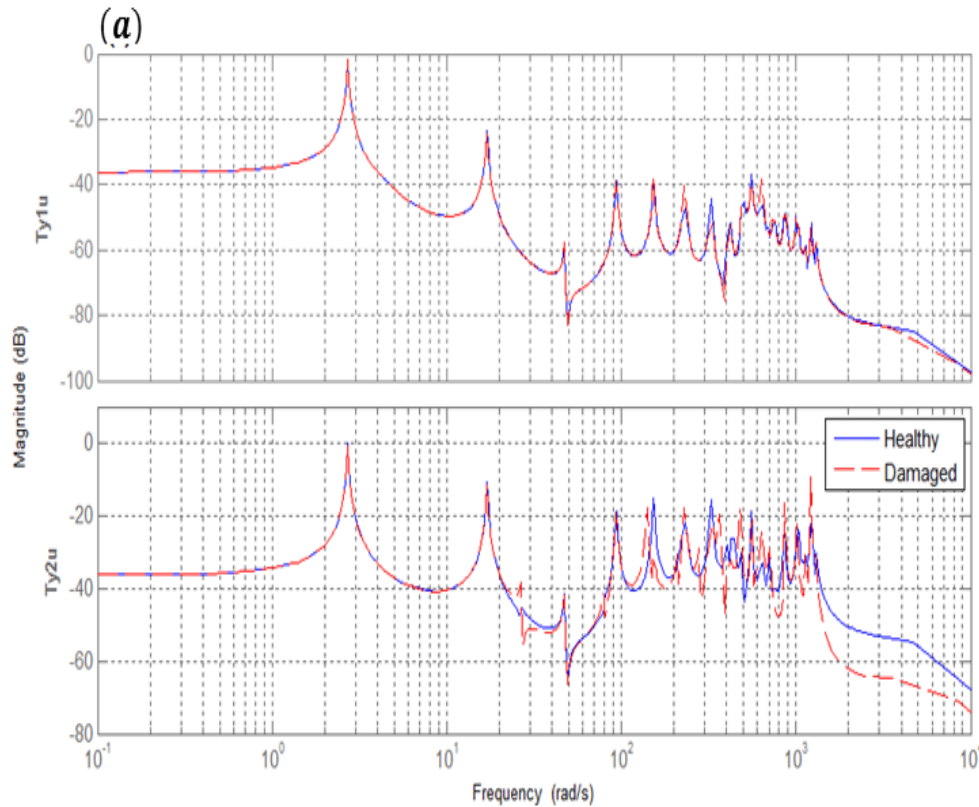
DTAC: A SPATIAL H_∞ CONTROL APPROACH

★ The spatial H_∞ control of the **healthy** structure



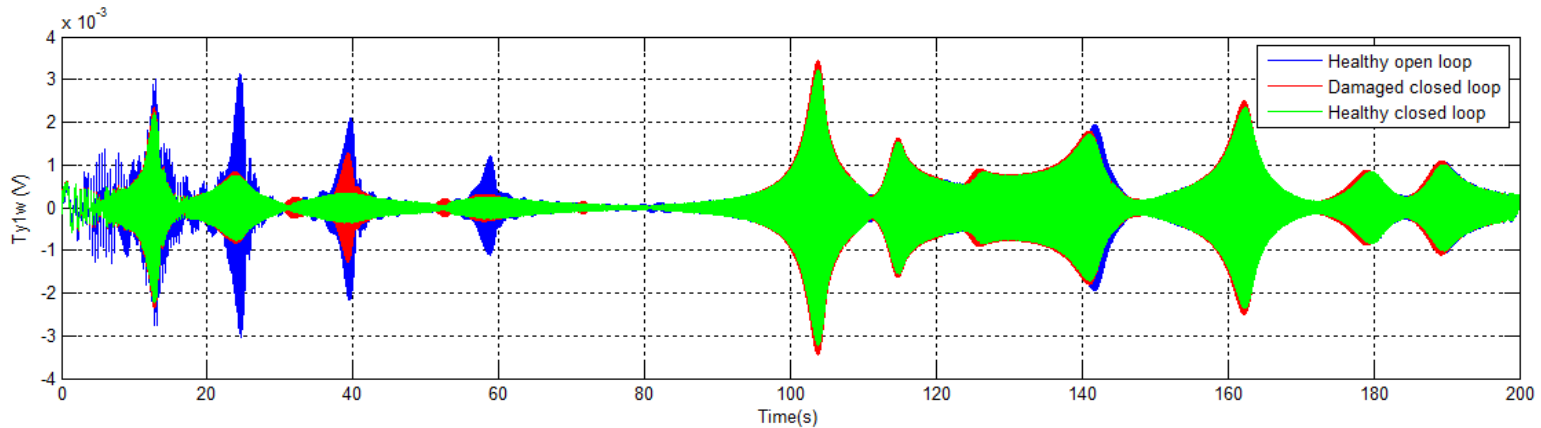
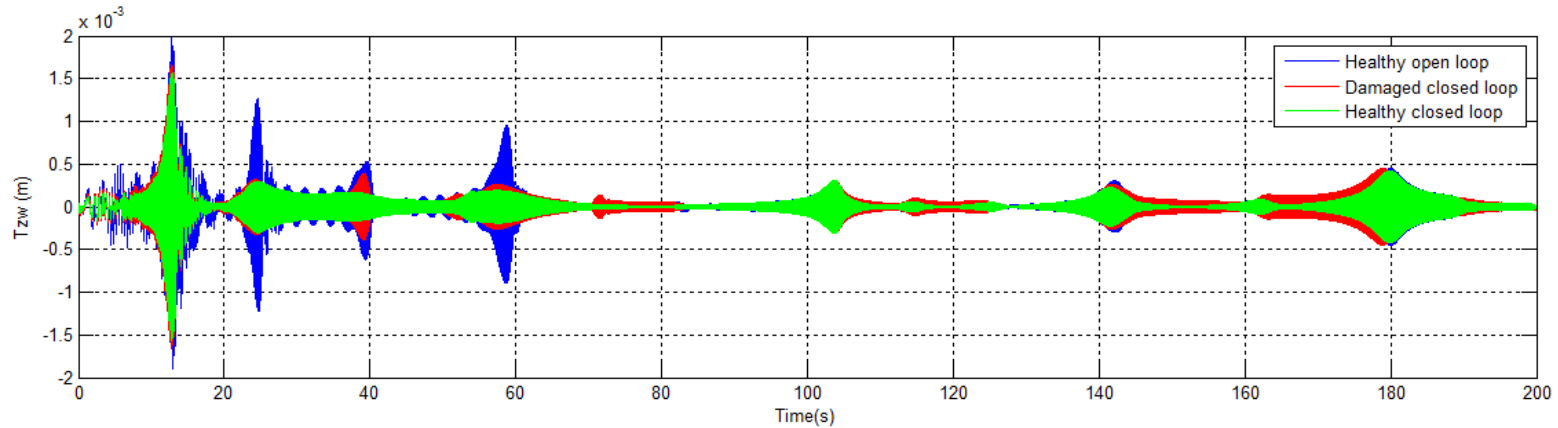
DTAC: A SPATIAL H_∞ CONTROL APPROACH

- ✿ **Robust controller: Small damage (Barely Visible Impact Damage - BVID)**



DTAC: A SPATIAL H_∞ CONTROL APPROACH

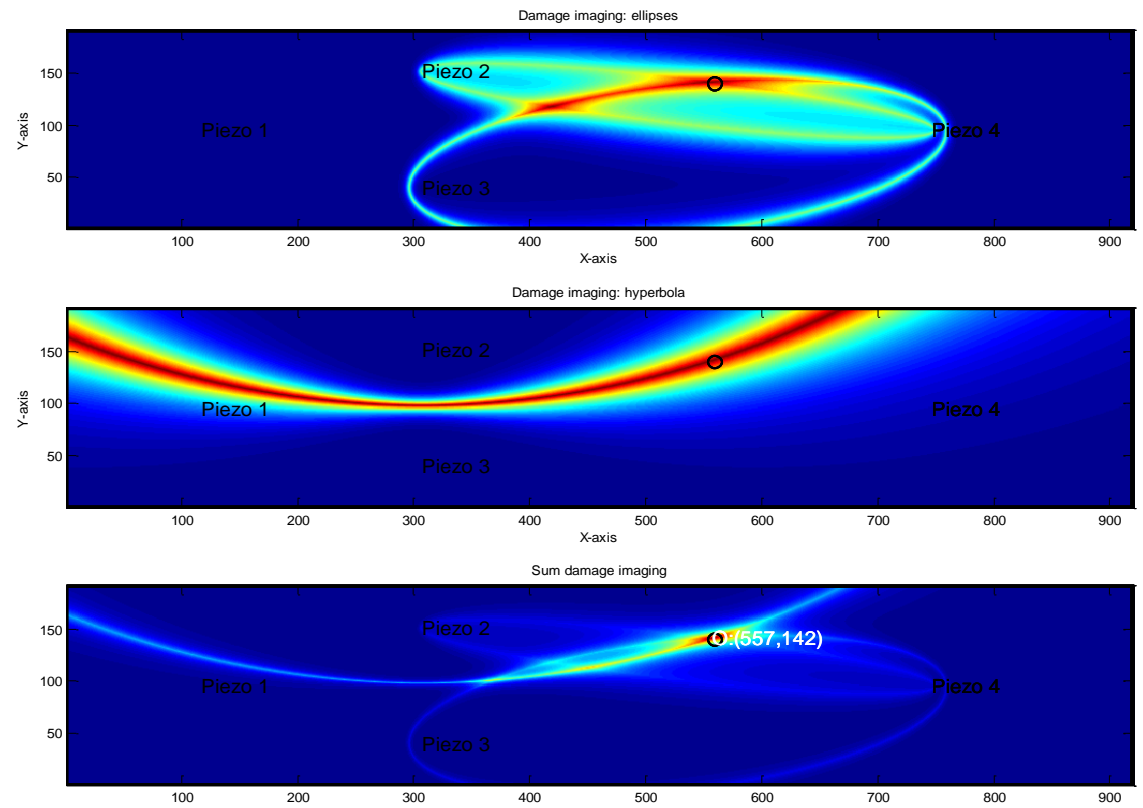
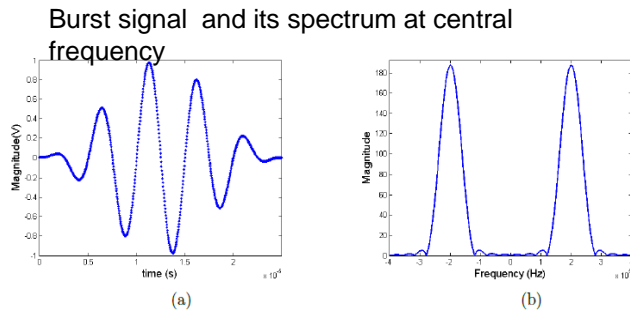
★ Robust controller - small damage (BVID)



DTAC: A SPATIAL H_∞ CONTROL APPROACH

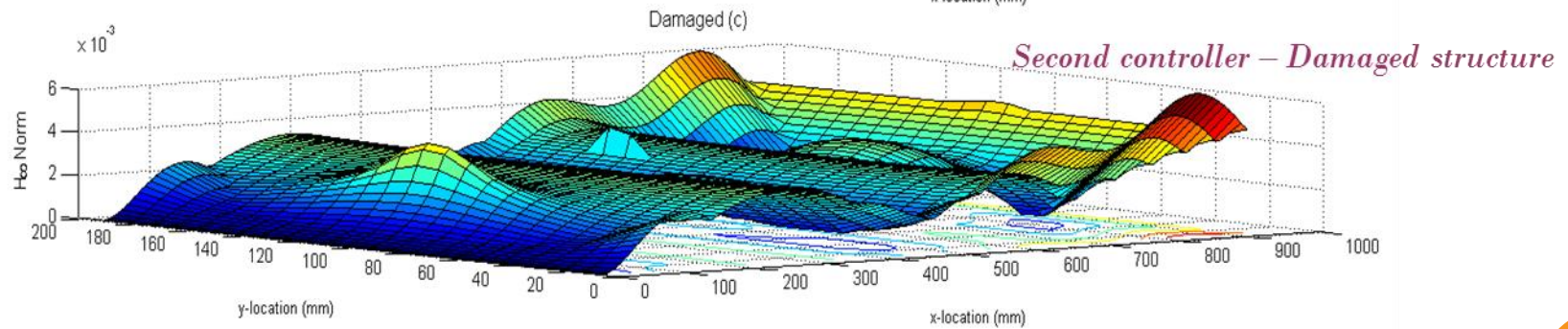
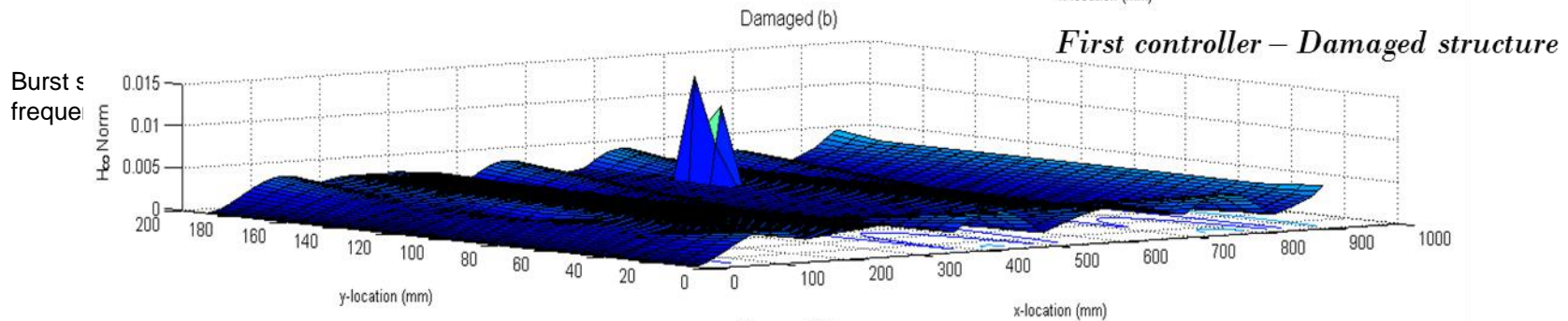
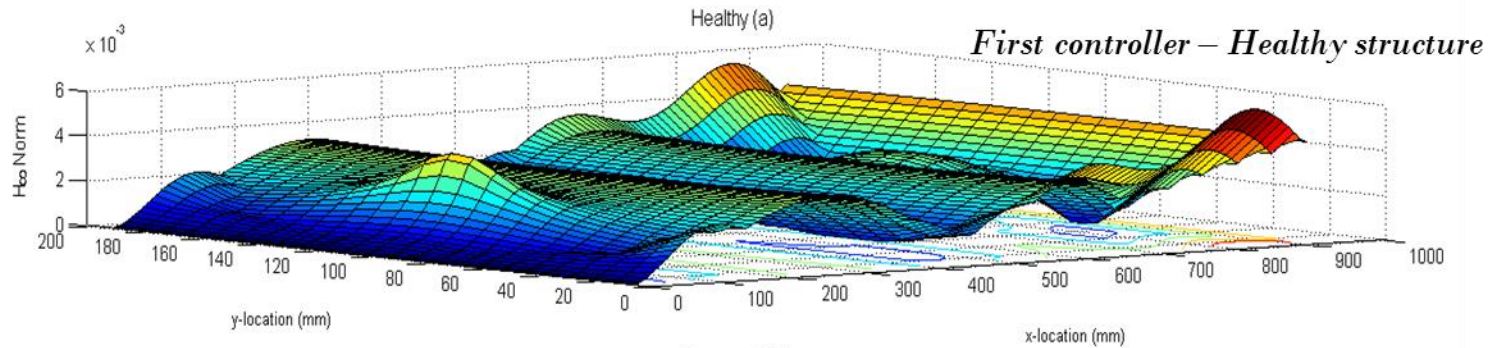
Reconfigurable controller – Severe damage

➤ Damage localization approach: Lamb waves-based damage localization



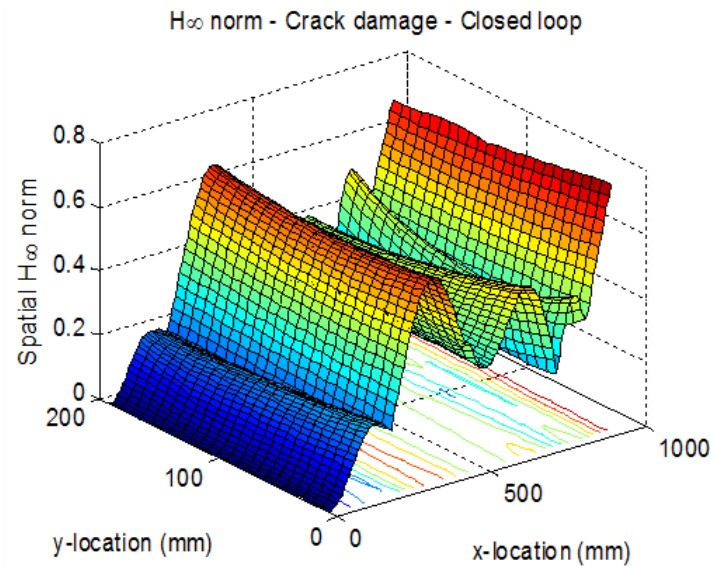
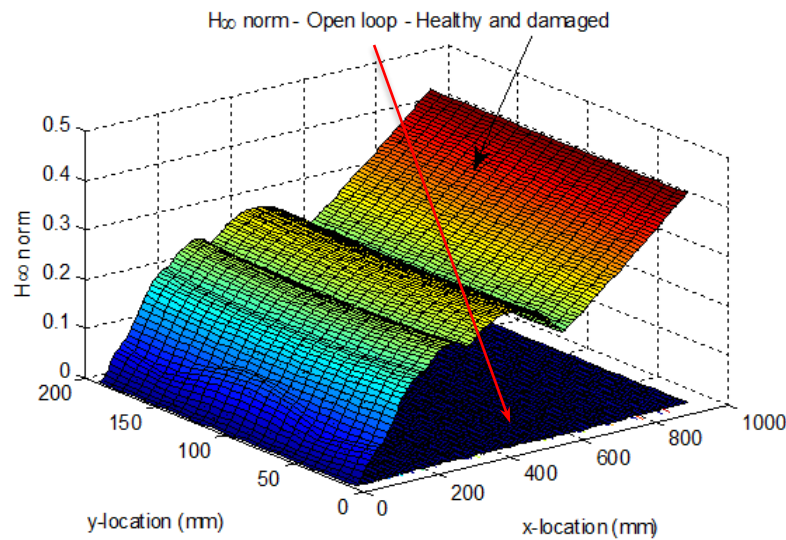
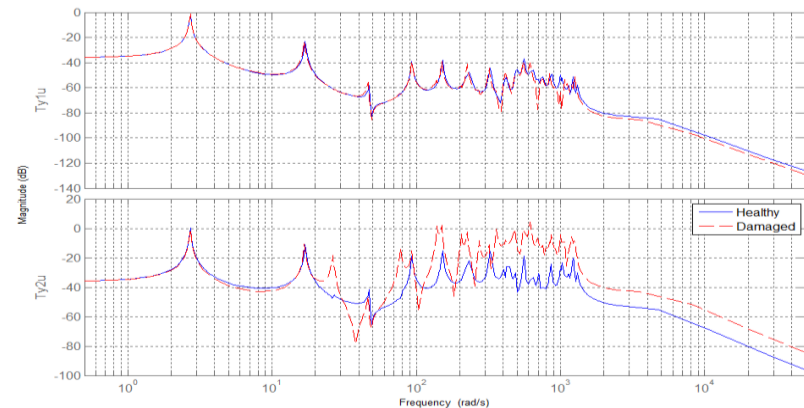
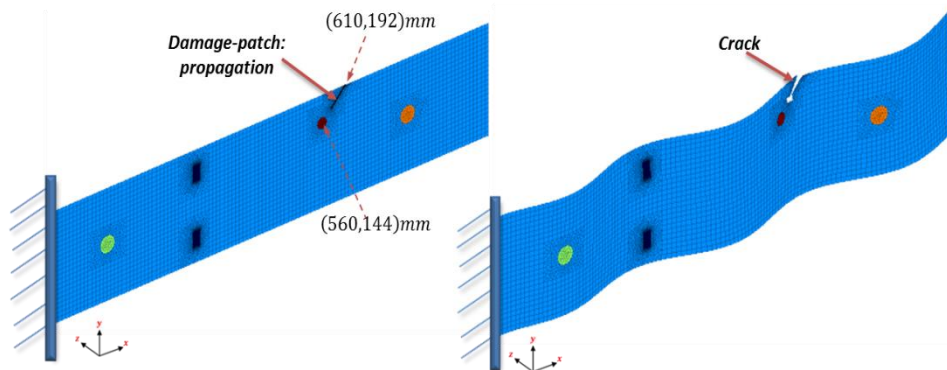
DTAC: A SPATIAL H_∞ CONTROL APPROACH

Reconfigurable controller – Severe damage



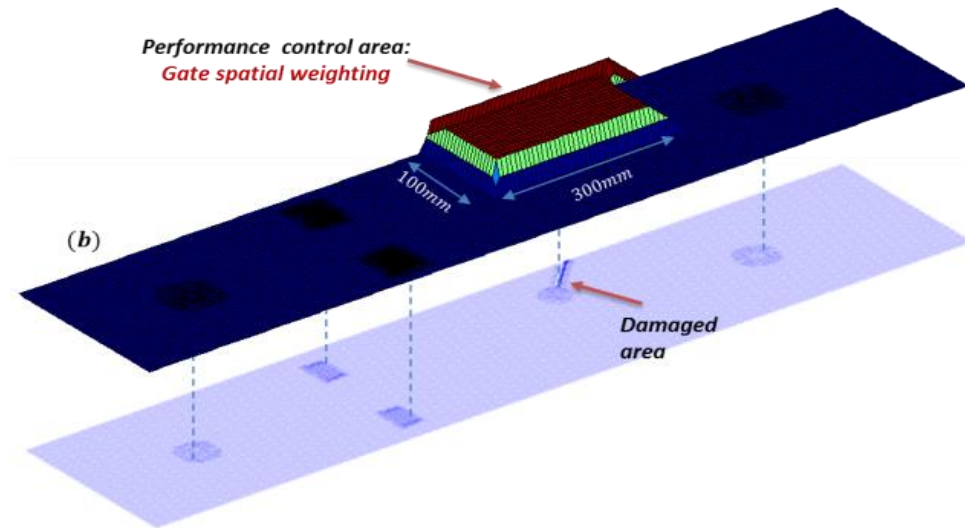
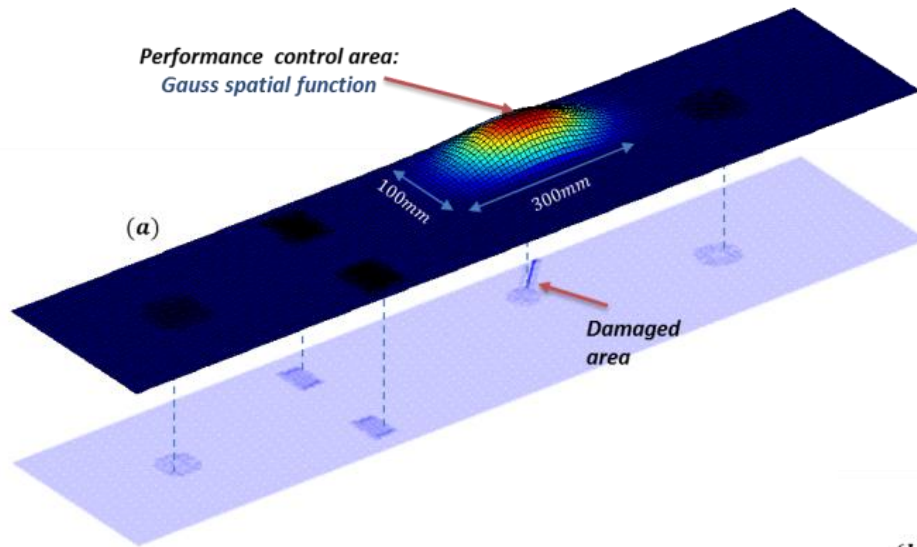
DTAC: A SPATIAL H_∞ CONTROL APPROACH

★ Evolving controller – Crack damage



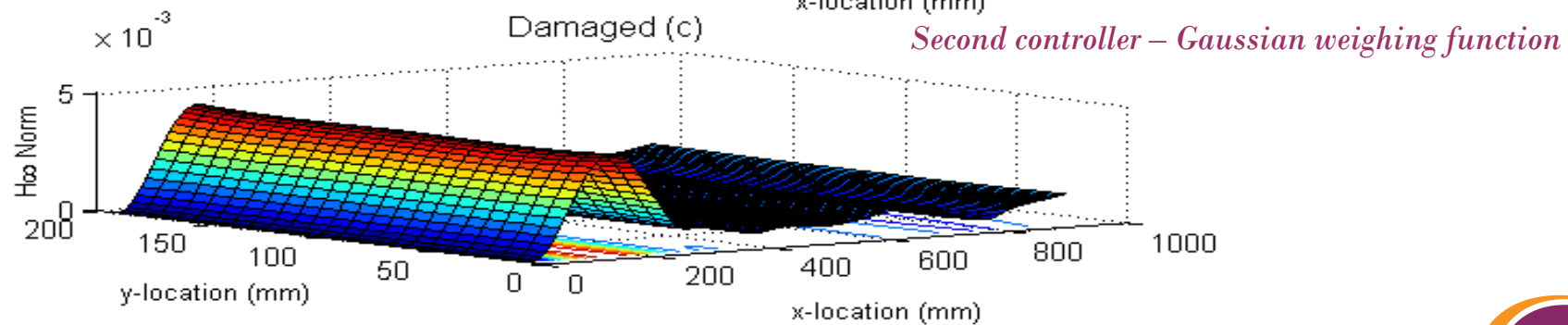
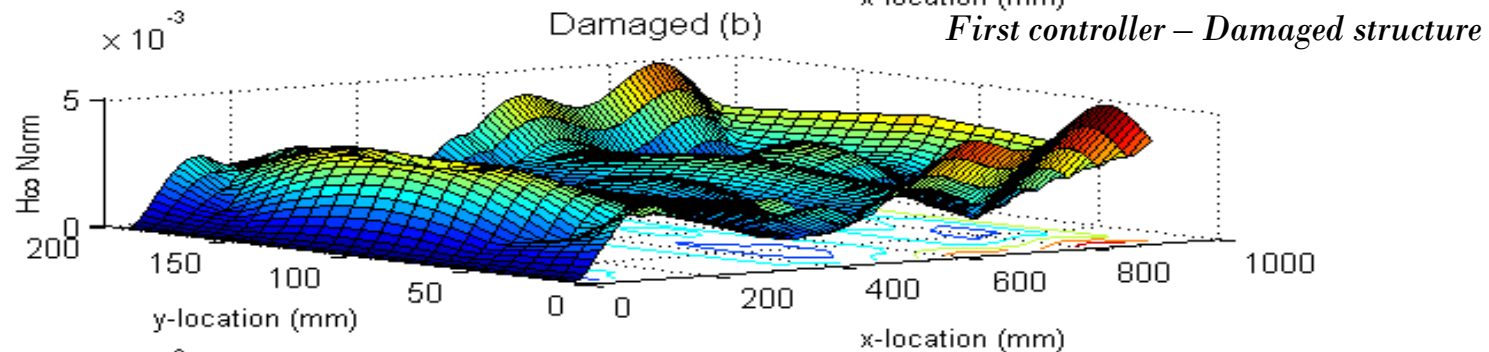
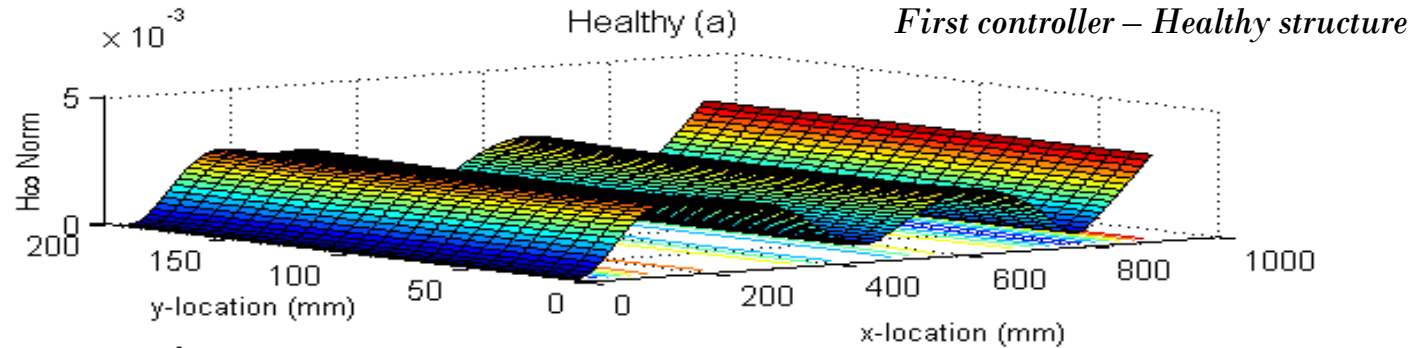
DTAC: A SPATIAL H_∞ CONTROL APPROACH

✿ Evolving controller – Spatial weighting functions



DTAC: A SPATIAL H_∞ CONTROL APPROACH

✿ Evolving controller – Spatial weighting functions





- **Introduction and Motivation**
- **Damage Tolerant Active Control (DTAC)**
- **DTAC strategies: Examples**
- **Conclusion**

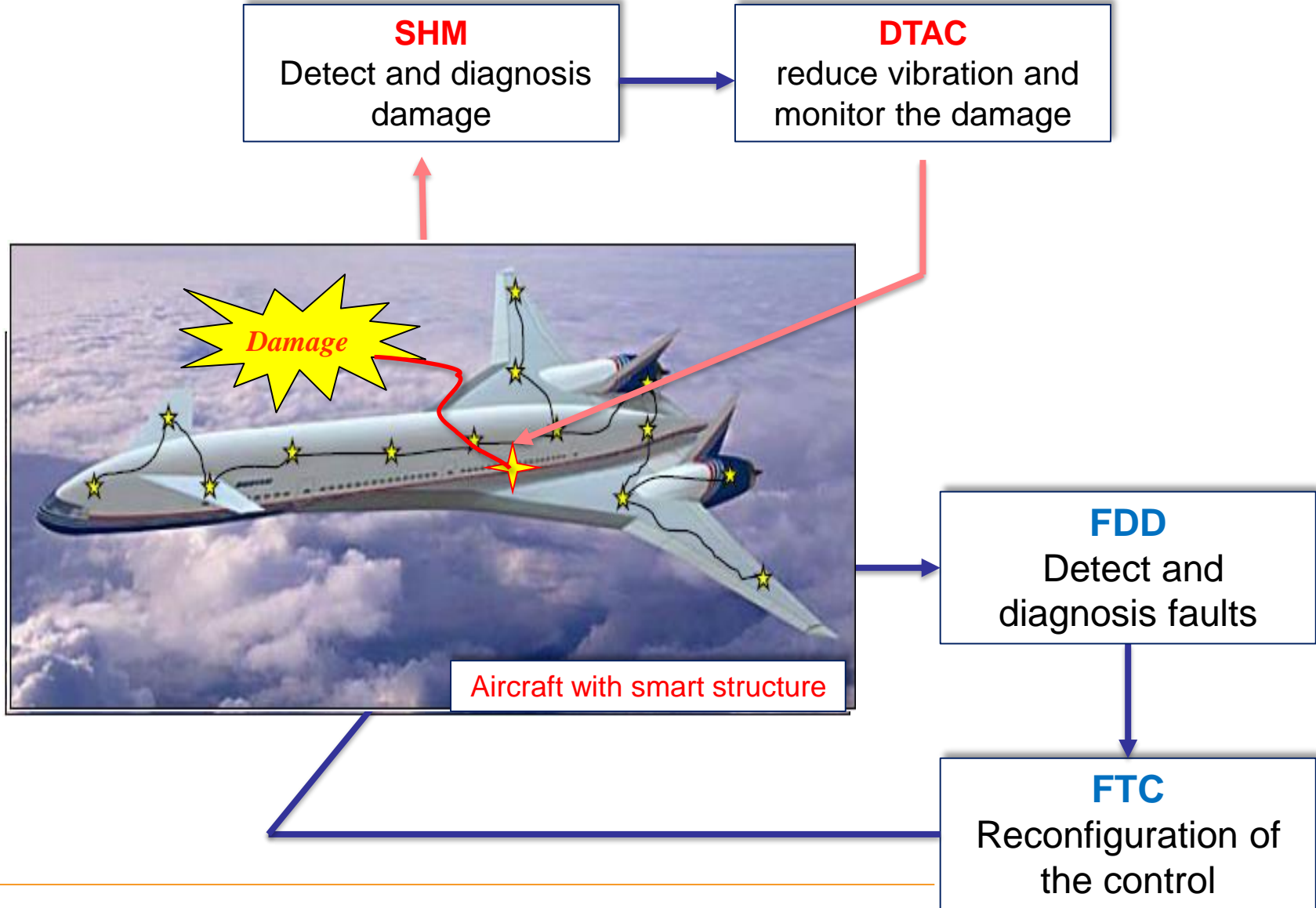
CONCLUSION

- ✿ A new paradigm to design fault tolerant controllers, specifically dedicated to face structural damages, was here examined, and called damage tolerant active control, or DTAC.
- ✿ Calls for FTC, SHM and active control of vibrations considering their interfaces with the introduced area of DTAC.
- ✿ Several techniques used in these areas are possible to be used to DTAC purpose, and main objectives and architectures to be adopted were discussed.
- ✿ On going works: theoretical investigation and experimental applications of the concepts and controller configurations are expected to be thoroughly studied to confirm the raised expectations
- ✿ New improvements: *fatigue and stress mitigation controllers*

DTAC NEW CONCEPT ?



DTAC and FTC interactions





FIN